## Physics 111

## Exam \#3

## March 1, 2024

Name $\qquad$

Please read and follow these instructions carefully:

- Read all problems carefully before attempting to solve them.
- Your work must be legible, and the organization clear.
- You must show all work, including correct vector notation.
- You will not receive full credit for correct answers without adequate explanations.
- You will not receive full credit if incorrect work or explanations are mixed in with correct work. Erase or cross out anything you don't want graded.
- Make explanations complete but brief. Do not write a lot of prose.
- Include diagrams.
- Show what goes into a calculation, not just the final number. For example, $|\vec{p}| \approx m|\vec{v}|=(5 \mathrm{~kg}) \times\left(2 \frac{\mathrm{~m}}{\mathrm{~s}}\right)=10 \frac{\mathrm{~kg} \cdot \mathrm{~m}}{\mathrm{~s}}$
- Give standard SI units with your results unless specifically asked for a certain unit.
- Unless specifically asked to derive a result, you may start with the formulas given on the formula sheet including equations corresponding to the fundamental concepts.
- Go for partial credit. If you cannot do some portion of a problem, invent a symbol and/or value for the quantity you can't calculate (explain that you are doing this), and use it to do the rest of the problem.
- Each free-response part is worth 6 points.

| Problem \#1 | $/ 24$ |
| :--- | :---: |
| Problem \#2 | $/ 24$ |
| Problem \#3 | $/ 24$ |
| Total | $/ 72$ |

I affirm that I have carried out my academic endeavors with full academic honesty.

1. Consider the side-view of a circuit in which a bar of mass $m=500 \mathrm{~g}$, length $L=10 \mathrm{~cm}$ and resistance $R=100 \Omega$ slides across a set of frictionless U-shaped horizontal rails as shown below. The bar is attached by a massless string that passes over a massless pulley to a $m_{h}=10 \mathrm{~g}$ hanging mass and the masses are both released from rest. A uniform magnetic field of magnitude $B$ points out through the loop and is oriented at $\theta=10^{0}$ to the right of vertical.

a. When the bar slides to the right across the rails there is a change in magnetic flux through the loop defined by the location of the bar at any moment in time. Explain whether the magnetic flux is increasing or decreasing and what is the direction of the current flowing in the bar as viewed from the side shown in the figure. In other words, is the current flowing in the bar coming towards me out of the paper or into the paper away from me?
b. When the bar reaches a terminal speed $v=1.5 \frac{\mathrm{~m}}{\mathrm{~s}}$, what is the tension in the string?
c. What is the magnitude of the constant external magnetic field $B$ ?
d. What is the energy dissapated per second in the bar?
2. A compound microscope containing two lenses is used to image Heterocarpus ensifer shrimp in a dish of water ( $n_{w}=1.33$ ). The objective lens (the lens closest to the shrimp in the dish) has a focal length $f_{o}=15 \mathrm{~mm}$ and is separated from the eyepiece by a distance $D=45 \mathrm{~mm}$. The image of the shrimp is projected through the eyepiece onto a screen 1.2 m away. In the dish, the shrimp is located 10 mm from the objective lens and its image on the screen is 150 mm in height. Note: The photos in this problem are adapted from those of Sönke Johnsen and Katie Thomas located at: https://oceanexplorer.noaa.gov/explorations/15biolum/logs/july23/july23.html.

a. What is the value of the focal length of the eyepiece, $f_{e}$ ?
b. How big is the shrimp in the dish?
c. In the image on the right of the shrimp on the screen, the shrimp appears to emit some bioluminescent fluid (the blue liquid) against a black background. The blue light has a wavelength of $\lambda=300 \mathrm{~nm}$ in the water with an intensity of $130 \frac{\mathrm{~W}}{\mathrm{~m}^{2}}$. What is the frequency of the emitted light and the maximum values of the electric and magnetic fields in the light?

d. Explain how you could tell if the bioluminescent light emitted were polarized or not and if it is polarized, the direction of polarization. To earn full credit be sure to fully explain your answer.
3. Tungsten x-rays are used in a Compton effect experiment. The incident tungsten xrays have an energy 59.3182 keV and are observed to scatter from stationary electrons at an angle $\phi$ measured counterclockwise with respect to the incident direction of the x-ray beam, taken to be long the horizontal at an angle of $0^{0}$.
a. If the electrons were known to scatter at an angle $\theta=31.5^{\circ}$ below the horizontal with a speed $v=0.176 c$, what was the energy of the scattered x-rays?
b. At what angle $\phi$ was the x-ray detector placed?
c. Suppose instead of using the tungsten x-rays in a Compton effect experiment, the x-rays were used in a photoelectric effect experiment where the x-rays are incident on electrons in a lead ( $\phi=4.14 \mathrm{eV}$ ) target with an intensity $S=1.2 \frac{\mathrm{~mW}}{\mathrm{~m}^{2}}$. How many photons per second are incident on the lead target if the beam on the lead target makes a spot 2 mm in diameter?
d. Are electrons ejected from the lead target by the tungsten x-rays? To earn full credit, you must show a calculation or explain your answer in full unambiguous detail?

Electrostatics
$F=k \frac{q_{1} q_{2}}{r^{2}}$
$\vec{F}=q \vec{E} ; \quad E_{p c}=k \frac{q}{r^{2}} ; \quad E_{\text {plate }}=\frac{q}{\epsilon_{0} A}$
$E=-\frac{\Delta V}{\Delta x}$
$V_{p c}=k \frac{q}{r}$
$U_{e}=k \frac{q_{1} q_{2}}{r}=q V$
$W=-q \Delta V=-\Delta U_{e}=\Delta K$
Electric Circuits - Capacitors
$Q=C V ; \quad C=\frac{\kappa \epsilon_{0} A}{d}$
$C_{\text {parallel }}=\sum_{i=1}^{N} C_{i}$
$\frac{1}{C_{\text {series }}}=\sum_{i=1}^{N} \frac{1}{C_{i}}$
$Q_{\text {charging }}(t)=Q_{\max }\left(1-e^{-\frac{t}{\tau}}\right)$
$Q_{\text {discharging }}(t)=Q_{\max } e^{-\frac{t}{\tau}}$
$I(t)=I_{\max } e^{-\frac{t}{\tau}}=\frac{Q_{\max }}{\tau} e^{-\frac{t}{\tau}}$
$\tau=R C$
$U_{C}=\frac{1}{2} q V=\frac{1}{2} C V^{2}=\frac{Q^{2}}{2 C}$
Light as a Wave
$c=f \lambda$
$S(t)=\frac{\text { Energy }}{\text { time } \times \text { Area }}=c \epsilon_{0} E^{2}(t)=c \frac{B^{2}(t)}{\mu_{0}}$
$I=S_{a v g}=\frac{1}{2} c \epsilon_{0} E_{\text {max }}^{2}=c \frac{B_{\text {max }}^{2}}{2 \mu_{0}}$
$P= \begin{cases}\frac{s}{c} ; & \text { absorbed } \\ \frac{2 S}{c} ; & \text { reflected }\end{cases}$
$S=S_{0} \cos ^{2} \theta$
$v=\frac{c}{n}$
$\theta_{\text {incident }}=\theta_{\text {reflected }}$
$n_{1} \sin \theta_{1}=n_{2} \sin \theta_{2}$
$P=\frac{1}{f}=\frac{1}{d_{0}}+\frac{1}{d_{i}}$
$M=\frac{d_{i}}{d_{0}} ; \quad|M|=\frac{h_{i}}{h_{0}}$

Magnetism
$\vec{F}=q \vec{v} \times \vec{B} \rightarrow F=q v B \sin \theta$
$\vec{F}=I \vec{L} \times \vec{B} \rightarrow F=I L B \sin \theta$
$V_{\text {Hall }}=w v_{d} B$
$B=\frac{\mu_{0} I}{2 \pi r}$
$\varepsilon=\Delta V=-N \frac{\Delta \phi_{B}}{\Delta t}$
$\phi_{B}=B A \cos \theta$
Electric Circuits - Resistors
$I=\frac{\Delta Q}{\Delta t}$
$I=n e A v_{d} ; \quad n=\frac{\rho N_{A}}{m}$
$V=I R$
$R=\frac{\rho L}{A}$
$R_{\text {series }}=\sum_{i=1}^{N} R_{i}$
$\frac{1}{R_{\text {parallel }}}=\sum_{i=1}^{N} \frac{1}{R_{i}}$
$P=\frac{\Delta E}{\Delta t}=I V=I^{2} R=\frac{V^{2}}{R}$

Light as a Particle/Relativity
$E=h f=\frac{h c}{\lambda}$
$K_{\text {max }}=h f-\phi$
$\Delta \lambda=\lambda^{\prime}-\lambda=\frac{h}{m c}(1-\cos \phi)$
$\frac{1}{E^{\prime}}=\frac{1}{E}+\frac{(1-\cos \phi)}{E_{\text {rest }}} ; \quad E_{\text {rest }}=m c^{2}$
$\gamma=\frac{1}{\sqrt{1-\frac{v^{2}}{c^{2}}}}$
$p=\gamma m v$
$E_{\text {total }}=E_{\text {rest }}+K=\gamma m c^{2}$
$K=(\gamma-1) m c^{2}$
$E_{\text {total }}^{2}=p^{2} c^{2}+m^{2} c^{4}$

Nuclear Physics

$$
\begin{aligned}
& N=N_{0} e^{-\lambda t} \\
& m=m_{0} e^{-\lambda t} \\
& A=A_{0} e^{-\lambda t} \\
& A=\lambda N \\
& t_{\frac{1}{2}}=\frac{\ln 2}{\lambda}
\end{aligned}
$$

## Constants

$g=9.8 \frac{m}{s^{2}}$
$1 e=1.6 \times 10^{-19} \mathrm{C}$
$k=\frac{1}{4 \pi \epsilon_{0}}=9 \times 10^{9} \frac{\mathrm{Nm}^{2}}{\mathrm{C}^{2}}$
$\epsilon_{0}=8.85 \times 10^{-12} \frac{\mathrm{c}^{2}}{\mathrm{Nm}^{2}}$
$1 \mathrm{eV}=1.6 \times 10^{-19} \mathrm{~J}$
$\mu_{0}=4 \pi \times 10^{-7 \frac{T m}{A}}$
$c=3 \times 10^{8} \frac{\mathrm{~m}}{\mathrm{~s}}$
$h=6.63 \times 10^{-34} \mathrm{Js}=4.14 \times 10^{-15} \mathrm{eVs}$
$N_{A}=6.02 \times 10^{23}$
$1 u=1.66 \times 10^{-27} \mathrm{~kg}=931.5 \frac{\mathrm{MeV}}{\mathrm{c}^{2}}$
$m_{p}=1.67 \times 10^{-27} \mathrm{~kg}=937.1 \frac{\mathrm{MeV}}{\mathrm{c}^{2}}$
$m_{n}=1.69 \times 10^{-27} \mathrm{~kg}=948.3 \frac{\mathrm{MeV}}{\mathrm{c}^{2}}$
$m_{e}=9.11 \times 10^{-31} \mathrm{~kg}=0.511 \frac{\mathrm{MeV}}{\mathrm{c}^{2}}$

Physics 110 Formulas

$$
\begin{aligned}
& \vec{F}=m \vec{a} ; \quad F_{G}=\frac{G M_{1} m_{2}}{r^{2}} ; \quad F_{s}=-k y ; \quad a_{c}=\frac{v^{2}}{r} \\
& W=-\Delta U_{g}-\Delta U_{s}=\Delta K \\
& U_{g}=m g y \\
& U_{s}=\frac{1}{2} k y^{2} \\
& K=\frac{1}{2} m v^{2} \\
& \vec{r}_{f}=\vec{r}_{i}+\vec{v}_{i} t+\frac{1}{2} \vec{a} t^{2} \\
& \vec{v}_{f}=\vec{v}_{i}+\vec{a} t \\
& v_{f}^{2}=v_{i}^{2}+2 a_{r} \Delta r
\end{aligned}
$$

## Common Metric Units

$$
\begin{aligned}
& \text { nano }(n)=10^{-9} \\
& \text { micro }(\mu)=10^{-6} \\
& \operatorname{milli}(m)=10^{-3} \\
& \operatorname{centi}(c)=10^{-2} \\
& \operatorname{kilo}(k)=10^{3} \\
& \operatorname{mega}(M)=10^{6}
\end{aligned}
$$

## Geometry/Algebra

| Circles: | $A=\pi r^{2}$ | $C=2 \pi r=\pi$ |
| :--- | :--- | :--- |
| Spheres: | $A=4 \pi r^{2} \quad V=\frac{4}{3} \pi r^{3}$ |  |
| Triangles: | $A=\frac{1}{2} b h$ |  |
| Quadratics: | $a x^{2}+b x+c=0 \rightarrow x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$ |  |

## PERIODIC TABLE OF ELEMENTS



