

Name \_\_\_\_\_  
 Physics 120 Quiz #2, April 8, 2011

Please show all work, thoughts and/or reasoning in order to receive partial credit. The quiz is worth 10 points total.

1. Suppose that the motion of a fan cart along a horizontal track is investigated and the horizontal motion is shown in the graph below. What can you say about the horizontal motion of the cart?



- The cart moves to the right gradually speeding up.
  - The cart moves to the right gradually slowing down.
  - The cart moves to the left gradually slowing down.
  - The cart moves to the right gradually slowing down, stops and starts moving to the left speeding up.
  - The cart moves to the left gradually slowing down, stops and starts moving to the right speeding up.
2. A small space probe, of mass  $240\text{kg}$ , is launched from a spacecraft near Mars. It travels toward the surface of Mars where it will land. At a time  $20.7\text{s}$  after it is launched, the probe is at the location  $\langle 4.3 \times 10^3, 8.7 \times 10^2, 0 \rangle \text{m}$  and at this same time its momentum is  $\langle 4.4 \times 10^4, -7.6 \times 10^3, 0 \rangle \frac{\text{kgm}}{\text{s}}$ . At this instant, the net force on the probe due to the gravitational pull of Mars plus the air resistance acting on the probe is  $\langle -7.0 \times 10^3, -9.2 \times 10^2, 0 \rangle \text{N}$ .

- a. Assuming that the net force on the probe is approximately constant over this time interval, what is the momentum of the probe  $20.9\text{s}$  after it is launched?

$$\vec{p}_f = \vec{p}_i + \vec{F}_{net} \Delta t = \langle 4.4 \times 10^4, -7.6 \times 10^3, 0 \rangle \frac{\text{kgm}}{\text{s}} + \langle -7.0 \times 10^3, -9.2 \times 10^2, 0 \rangle \times 0.2 \text{Ns}$$

$$\vec{p}_f = \langle 4.26 \times 10^4, -7.78 \times 10^3, 0 \rangle \frac{\text{kgm}}{\text{s}}$$

- b. What is the location of the probe  $20.9\text{s}$  after launch? (Hint: you will need to calculate  $v_{avg}$ .)

$$\vec{r}_f = \vec{r}_i + \vec{v}_{avg} \Delta t = \vec{r}_i + \left[ \frac{\vec{v}_i + \vec{v}_f}{2} \right] \Delta t = \vec{r}_i + \left[ \frac{\vec{p}_i + \vec{p}_f}{2m} \right] \Delta t$$

$$\vec{r}_f = \langle 4.3 \times 10^3, 8.7 \times 10^2, 0 \rangle \text{m} + \left[ \frac{\langle 4.4 \times 10^4, -7.6 \times 10^3, 0 \rangle \frac{\text{kgm}}{\text{s}} + \langle 4.26 \times 10^4, -7.78 \times 10^3, 0 \rangle \frac{\text{kgm}}{\text{s}}}{2 \times 240 \text{kg}} \right] \times 0.2 \text{s}$$

$$\vec{r}_f = \langle 4336, 864, 0 \rangle \text{m}$$

**Useful formulas:**

$$\vec{p} = \gamma m \vec{v}$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$$\vec{v}_{avg} = \frac{\vec{v}_i + \vec{v}_f}{2}$$

**Momentum Principle:**  $\vec{p}_f = \vec{p}_i + \vec{F}_{net} \Delta t$

**Position-update:**  $\vec{r}_f = \vec{r}_i + \vec{v}_{avg} \Delta t = \vec{r}_i + \frac{\vec{p}}{m \sqrt{1 + \frac{p^2}{m^2 c^2}}} \Delta t$

**Geometry /Algebra**

*Circles      Triangles      Spheres*

$$C = 2\pi r \quad A = \frac{1}{2}bh \quad A = 4\pi r^2$$

$$A = \pi r^2 \quad V = \frac{4}{3}\pi r^3$$

Quadratic equation:  $ax^2 + bx + c = 0$ ,

whose solutions are given by:  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

**Vectors**

magnitude of a vector:  $|\vec{a}| = \sqrt{a_x^2 + a_y^2 + a_z^2}$

writing a vector:  $\vec{a} = \langle a_x, a_y, a_z \rangle = |\vec{a}| \hat{a} = a_x \hat{i} + a_y \hat{j} + a_z \hat{k}$