Name
PIXE Homework #2 - Physics 100
Union College Fall 2017

1. Describe the PIXE process.

PIXE stands for proton induced x-ray emission spectroscopy. This is a technique whereby a high-energy proton interacts with a target nucleus ejecting an electron from an inner atomic orbital of the target atom. An electron from a higher atomic orbital de-excites to the vacancy in the lower atomic orbital with an emission of an x-ray photon. The energy of the photon is characteristic of the atomic nucleus.

2. What are the K_{α} and K_{β} transition energies for the following elements: ${}^{19}_{9}F$, ${}^{59}_{27}Co$, and ${}^{197}_{79}Au$? (Please use the equations given in the lecture and not the table of x-ray energies to do the calculation.)

The x-ray energies are given by
$$\Delta E = -Z^2 \frac{me^4}{2(4\pi\epsilon_0)^2 \hbar^2} \left(\frac{1}{n_l^2} - \frac{1}{n_u^2}\right)$$
, where for the α -

transition we have $n_u = 2 \rightarrow n_l = 1$ and for a β -transition $n_u = 3 \rightarrow n_l = 1$. Thus for a K_{α} transition (evaluating the constants) we have

$$\Delta E_{\alpha} = -Z^{2} \frac{me^{4}}{2(4\pi\epsilon_{0})^{2} \hbar^{2}} \left(\frac{1}{n_{l}^{2}} - \frac{1}{n_{u}^{2}}\right) = -Z^{2} \left[\frac{9.11 \times 10^{-31} kg \times \left(1.6 \times 10^{-19} C\right)^{4}}{32\pi^{2} \left(8.85 \times 10^{-12} \frac{C^{2}}{Nm^{2}}\right)^{2} \left(\frac{6.63 \times 10^{-34} Js}{2\pi}\right)^{2}} \right] \left(\frac{1}{1} - \frac{1}{4}\right) \Delta E_{\alpha} = \left(1.626 \times 10^{-18} J\right) Z^{2} = (10.16) Z^{2}$$

, while for a K_{β} transition

$$\Delta E_{\beta} = -Z^{2} \frac{me^{4}}{2(4\pi\varepsilon_{0})^{2} \hbar^{2}} \left(\frac{1}{n_{l}^{2}} - \frac{1}{n_{u}^{2}}\right) = -Z^{2} \left[\frac{9.11 \times 10^{-31} kg \times (1.6 \times 10^{-19} C)^{4}}{32\pi^{2} (8.85 \times 10^{-12} \frac{C^{2}}{Nm^{2}})^{2} \left(\frac{6.63 \times 10^{-34} Js}{2\pi}\right)^{2}}\right] \left(\frac{1}{1} - \frac{1}{9}\right)$$

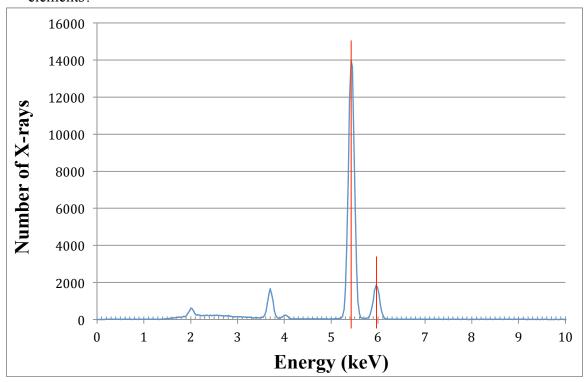
$$\Delta E_{\beta} = (1.927 \times 10^{-18} J)Z^{2} = (12.04 eV)Z^{2}$$

Element	$\Delta E_{\alpha} (keV)$	$\Delta E_{\alpha}(J)$	$\Delta E_{\beta} (keV)$	$\Delta E_{\beta}(J)$
$^{19}_{9}F$	0.822	1.31×10^{-16}	0	0
⁵⁹ ₂₇ Co	7.407	1.19×10^{-15}	8.78	1.40×10^{-15}
¹⁹⁷ ₇₉ A u	63.41	1.02×10^{-14}	75.14	1.20×10^{-14}

3. What is the ratio of the K_{α} energies of $^{238}_{92}U$ to $^{12}_{6}C$?

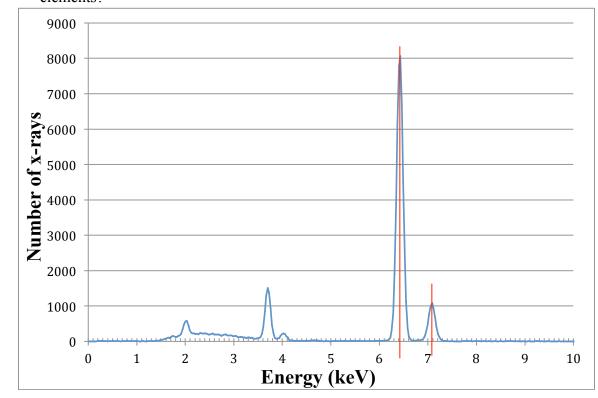
Using the formula above: $\frac{U_{K_{\alpha}}}{C_{K_{\alpha}}} = \frac{(92)^2}{(6)^2} = 235$ where all of the constants cancel by taking the ratio.

4. Given the *PIXE* spectrum of a single element standard shown below, what are the elements?



The energy of the K_{α} peak is approximately 5.4keV, while the K_{α} peak is 6.0keV. Using the formula from problem #2 we can calculate the atomic number of the unknown element. Using the K_{α} energy, we have $\Delta E_{\alpha} = 5.4 \text{keV} = (10.16 \text{eV})Z^2 \rightarrow Z = 22.5$ and thus the element could be either Ti (Z = 22) or V(Z = 23). From the K_{β} energy, we have $\Delta E_{\beta} = 6.0 \text{keV} = (12.04 \text{eV})Z^2 \rightarrow Z = 22.4$ and thus the element could be either Ti (Z = 22) or V(Z = 23).

5. Given the *PIXE* spectrum of a single element standard shown below, what are the elements?



The energy of the K_{α} peak is approximately 6.4keV, while the K_{α} peak is 7.1keV. Using the formula from problem #2 we can calculate the atomic number of the unknown element. Using the K_{α} energy, we have $\Delta E_{\alpha} = 6.4$ keV = (10.16eV) $Z^2 \rightarrow Z = 25$ and thus the element could be Mn (Z = 25). From the K_{β} energy, we have $\Delta E_{\beta} = 7.1$ keV = (12.04eV) $Z^2 \rightarrow Z = 24.3$ and thus the element could be either Cr (Z = 24) or Mn (Z = 25).