

Name \_\_\_\_\_  
 PIXE Homework #2 - Physics 100  
 Union College Fall 2024

- Describe the PIXE process using words and/or diagrams. If you use a diagram, please explain what the diagram is about.

*PIXE stands for proton induced x-ray emission spectroscopy. This is a technique whereby a high-energy proton interacts with a target nucleus ejecting an electron from an inner atomic orbital of the target atom. An electron from a higher atomic orbital de-excites to the vacancy in the lower atomic orbital with an emission of an x-ray photon. The energy of the photon is characteristic of the atomic nucleus.*

- What are the  $K_\alpha$  and  $K_\beta$  transition energies for the following elements:  ${}^{40}_{20}\text{Ca}$ ,  ${}^{59}_{27}\text{Co}$ , and  ${}^{197}_{79}\text{Au}$ ? (Please use the equations given in the lecture and not the table of x-ray energies to do the calculation.)

The x-ray energies are given by  $\Delta E = -Z^2 \frac{me^4}{2(4\pi\epsilon_0)^2 \hbar^2} \left( \frac{1}{n_i^2} - \frac{1}{n_u^2} \right)$ , where for the  $\alpha$ -transition we have  $n_u = 2 \rightarrow n_i = 1$  and for a  $\beta$ -transition  $n_u = 3 \rightarrow n_i = 1$ . Thus, for a  $K_\alpha$  transition (evaluating the constants) we have

$$\Delta E_\alpha = -Z^2 \frac{me^4}{2(4\pi\epsilon_0)^2 \hbar^2} \left( \frac{1}{n_i^2} - \frac{1}{n_u^2} \right) = -Z^2 \left[ \frac{9.11 \times 10^{-31} \text{ kg} \times (1.6 \times 10^{-19} \text{ C})^4}{32\pi^2 \left( 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2} \right)^2 \left( \frac{6.63 \times 10^{-34} \text{ Js}}{2\pi} \right)^2} \right] \left( \frac{1}{1} - \frac{1}{4} \right)$$

$$\Delta E_\alpha = (1.626 \times 10^{-18} \text{ J}) Z^2 = (10.16) Z^2$$

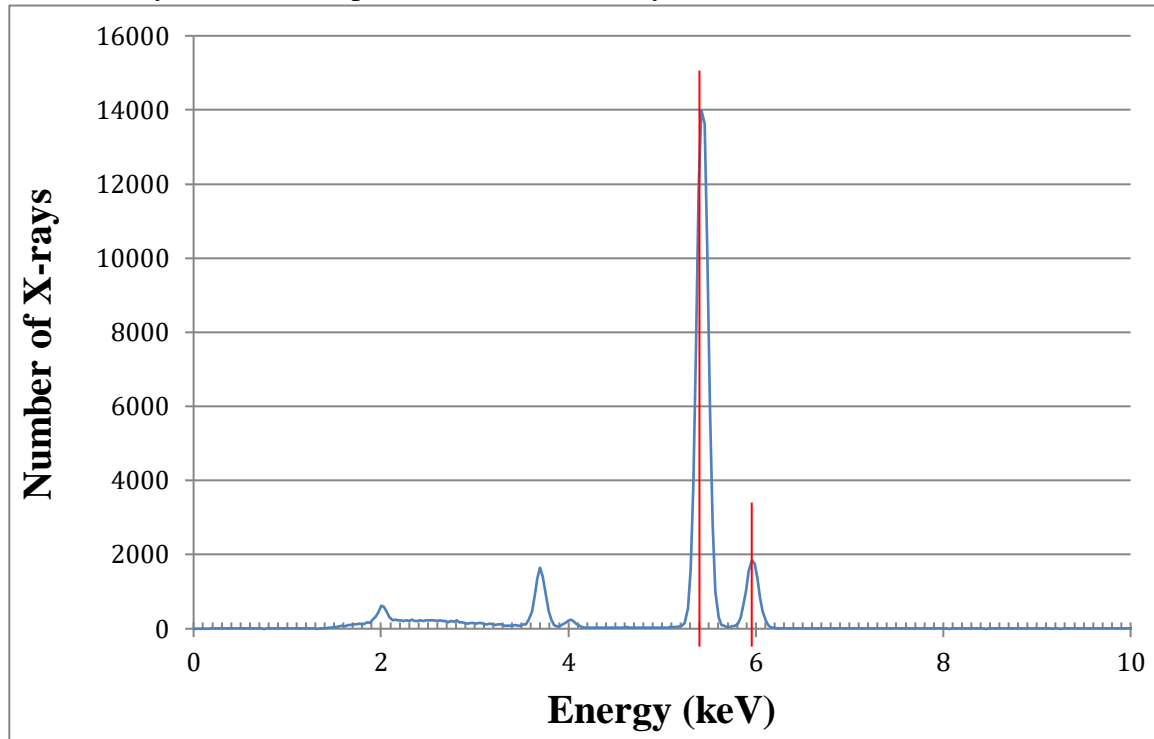
, while for a  $K_\beta$  transition

$$\Delta E_\beta = -Z^2 \frac{me^4}{2(4\pi\epsilon_0)^2 \hbar^2} \left( \frac{1}{n_i^2} - \frac{1}{n_u^2} \right) = -Z^2 \left[ \frac{9.11 \times 10^{-31} \text{ kg} \times (1.6 \times 10^{-19} \text{ C})^4}{32\pi^2 \left( 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2} \right)^2 \left( \frac{6.63 \times 10^{-34} \text{ Js}}{2\pi} \right)^2} \right] \left( \frac{1}{1} - \frac{1}{9} \right)$$

$$\Delta E_\beta = (1.927 \times 10^{-18} \text{ J}) Z^2 = (12.04 \text{ eV}) Z^2$$

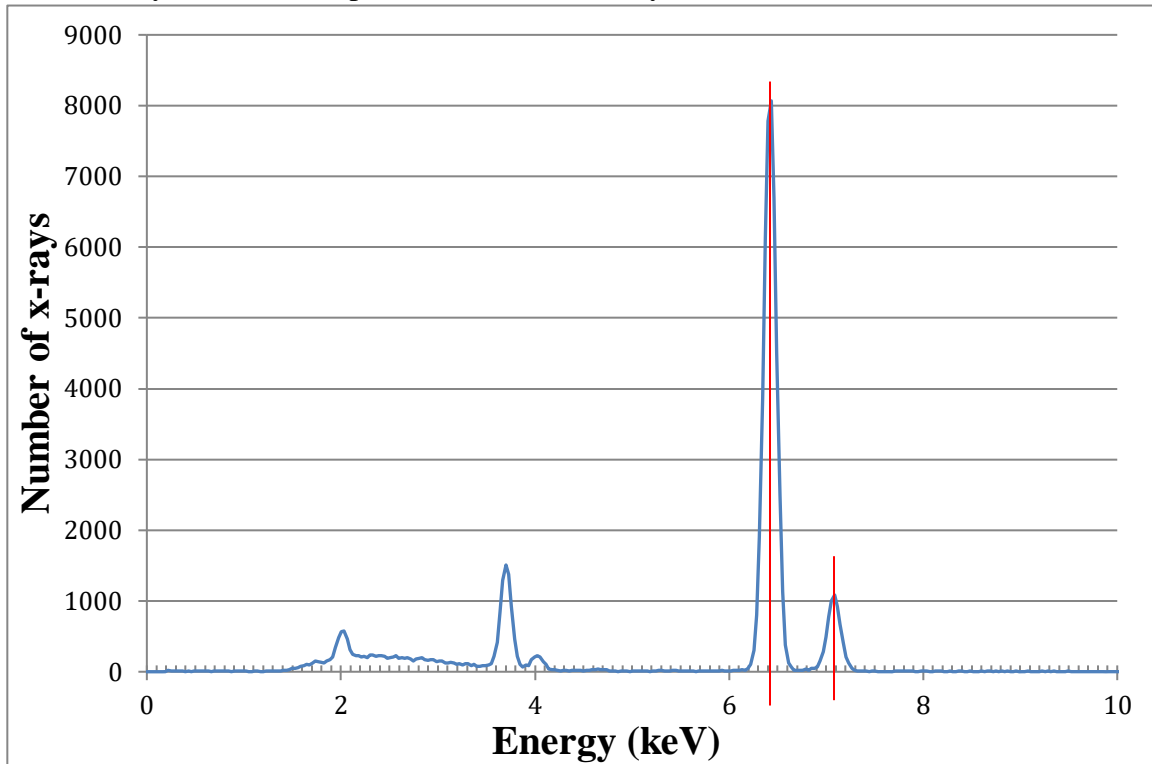
Element	$\Delta E_\alpha$ (keV)	$\Delta E_\alpha$ (J)	$\Delta E_\beta$ (keV)	$\Delta E_\beta$ (J)
${}^{40}_{20}\text{Ca}$	4.064	$6.5 \times 10^{-16}$	4.816	$7.7 \times 10^{-16}$
${}^{59}_{27}\text{Co}$	7.407	$1.19 \times 10^{-15}$	8.78	$1.4 \times 10^{-15}$
${}^{197}_{79}\text{Au}$	63.41	$1.02 \times 10^{-14}$	75.14	$1.2 \times 10^{-14}$

3. Given the *PIXE* spectrum of a single element standard shown below, what is the element indicated by the red lines? Hint: Approximate the energy of the peaks and use the unmodified energy equations to determine the atomic number of the element. You may need to use a periodic table to identify the element.



The energy of the  $K_a$  peak is approximately  $5.4\text{keV}$ , while the  $K_b$  peak is  $6.0\text{keV}$ . Using the formula from problem #2 we can calculate the atomic number of the unknown element. Using the  $K_a$  energy, we have  $\Delta E_a = 5.4\text{keV} = (10.16\text{eV})Z^2 \rightarrow Z = 22.5$  and thus the element could be either Ti ( $Z = 22$ ) or V ( $Z = 23$ ). From the  $K_b$  energy, we have  $\Delta E_b = 6.0\text{keV} = (12.04\text{eV})Z^2 \rightarrow Z = 22.4$  and thus the element could be either Ti ( $Z = 22$ ) or V ( $Z = 23$ ). Most likely we'd choose titanium.

4. Given the *PIXE* spectrum of a single element standard shown below, what is the element indicated by the red lines? Hint: Approximate the energy of the peaks and use the unmodified energy equations to determine the atomic number of the element. You may need to use a periodic table to identify the element.



The energy of the  $K_a$  peak is approximately  $6.4\text{keV}$ , while the  $K_b$  peak is  $7.1\text{keV}$ . Using the formula from problem #2 we can calculate the atomic number of the unknown element. Using the  $K_a$  energy, we have  $\Delta E_a = 6.4\text{keV} = (10.16\text{eV})Z^2 \rightarrow Z = 25$  and thus the element could be Mn ( $Z = 25$ ). From the  $K_b$  energy, we have  $\Delta E_b = 7.1\text{keV} = (12.04\text{eV})Z^2 \rightarrow Z = 24.3$  and thus the element could be either Cr ( $Z = 24$ ) or Mn ( $Z = 25$ ). We'd most likely choose chromium.