

Physics 111 Homework Solutions Week #9 - Wednesday

Friday, February 28, 2104

Chapters 19 & 24

Questions

24.6 The Compton shift in wavelength for the proton and the electron are given by

$$\Delta\lambda_p = \frac{h}{m_p c}(1 - \cos\phi) \text{ and } \Delta\lambda_e = \frac{h}{m_e c}(1 - \cos\phi) \text{ respectively. Evaluating the ratio}$$

of the shift in wavelength for the proton to the electron, evaluated at the same

detection angle ϕ , we find $\frac{\Delta\lambda_p}{\Delta\lambda_e} = \frac{m_e}{m_p} = \frac{1.67 \times 10^{-27} \text{ kg}}{9.11 \times 10^{-31} \text{ kg}} = \frac{1}{1833} = 5 \times 10^{-4}$. Therefore

the shift in wavelength for the proton is smaller than the wavelength shift for the electron.

Multiple-Choice

19.16 D

19.17 A

Problems

19.15 The frequency is given as $f = \frac{c}{\lambda} = \frac{3 \times 10^8 \frac{\text{m}}{\text{s}}}{5.5 \times 10^{-7} \text{ m}} = 5.5 \times 10^{14} \text{ s}^{-1}$.

19.17 A Neodymium-YAG laser

a. The number of photons is given as the total beam energy divided by the energy

$$\text{per photon, or } \# = \frac{5J}{\frac{hc}{\lambda}} = \frac{5J}{6.63 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \frac{\text{m}}{\text{s}}} \times 1.06 \times 10^{-6} \text{ m} = 1.33 \times 10^{20}.$$

b. The power in the beam is the energy delivered per unit time, or

$$P = \frac{\Delta E}{\Delta t} = \frac{5J}{1 \times 10^{-9} \text{ s}} = 5 \times 10^9 \text{ W} = 5 \text{ GW}.$$

c. The average power output of the laser is $P = \frac{5J}{\text{pulse}} \times \frac{10 \text{ pulses}}{1 \text{ s}} = 50 \text{ W}$.

19.18 The range of frequencies is given as $f_{400 \text{ nm}} = \frac{c}{\lambda_{400 \text{ nm}}} = \frac{3 \times 10^8 \frac{\text{m}}{\text{s}}}{400 \times 10^{-9} \text{ m}} = 7.5 \times 10^{14} \text{ Hz}$

through $f_{750 \text{ nm}} = \frac{c}{\lambda_{750 \text{ nm}}} = \frac{3 \times 10^8 \frac{\text{m}}{\text{s}}}{750 \times 10^{-9} \text{ m}} = 4 \times 10^{14} \text{ Hz}$. The energies are given by

$$E = \frac{hc}{\lambda} = hf \text{ which for } 750 \text{ nm the energy is}$$

$$E = \frac{(6.63 \times 10^{-34} \text{ Js})(3 \times 10^8 \frac{\text{m}}{\text{s}})}{750 \times 10^{-9} \text{ m}} = 2.65 \times 10^{-19} \text{ J} \times \frac{1 \text{ eV}}{1.6 \times 10^{-19} \text{ J}} = 1.66 \text{ eV} \text{ while the}$$

energy for the 400 nm photon is

$$E = \frac{(6.63 \times 10^{-34} \text{ Js})(3 \times 10^8 \frac{\text{m}}{\text{s}})}{400 \times 10^{-9} \text{ m}} = 4.97 \times 10^{-19} \text{ J} \times \frac{1 \text{ eV}}{1.6 \times 10^{-19} \text{ J}} = 3.11 \text{ eV}.$$

19.20 The energy of the emitted photon is equal to the difference in energies of the two levels: $\Delta E = -1.51 \text{ eV} - (-3.4 \text{ eV}) = 1.89 \text{ eV} \times \frac{1.6 \times 10^{-19} \text{ J}}{1 \text{ eV}} = 3.02 \times 10^{-19} \text{ J}$. Then

setting this energy equal to $\frac{hc}{\lambda}$ we find

$$\lambda = \frac{hc}{E} = \frac{6.63 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \frac{\text{m}}{\text{s}}}{3.02 \times 10^{-19} \text{ J}} = 6.58 \times 10^{-7} \text{ m} = 658 \text{ nm}.$$

19.21 Another Neodymium-YAG laser

a. Each photon has an energy given by

$$E = \frac{hc}{\lambda} = \frac{6.63 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \frac{\text{m}}{\text{s}}}{532 \times 10^{-9} \text{ m}} = 3.74 \times 10^{-19} \text{ J per photon. Similarly the}$$

momentum is $p = \frac{h}{\lambda} = \frac{6.63 \times 10^{-34} \text{ Js}}{532 \times 10^{-9} \text{ m}} = 1.25 \times 10^{-27} \frac{\text{kgm}}{\text{s}}$ per photon.

b. Since the total energy is 5J, we calculate the number of photos by dividing the total energy by the energy per photon. Thus we have

$$\# = \frac{E_{total}}{E/\text{photon}} = \frac{5 \text{ J}}{3.74 \times 10^{-19} \text{ J/photon}} = 1.34 \times 10^{19} \text{ photons.}$$

c. In 1 ns, if all the photons in part b are absorbed, each carrying a momentum p , then the force is the total change in momentum and is given by

$$F = N \frac{\Delta p}{\Delta t} = 1.34 \times 10^{19} \times \frac{1.25 \times 10^{-27} \frac{\text{kgm}}{\text{s}}}{1 \times 10^{-9} \text{ s}} = 16.7 \text{ N}.$$

24.7 For a $1.2 \times 10^6 \text{ eV} \times \frac{1.6 \times 10^{-19} \text{ J}}{1 \text{ eV}} = 1.92 \times 10^{-13} \text{ J photon}$,

a. its momentum is given by $p = \frac{E}{c} = \frac{1.92 \times 10^{-13} \text{ J}}{3 \times 10^8 \frac{\text{m}}{\text{s}}} = 6.4 \times 10^{-22} \frac{\text{kgm}}{\text{s}}$.

b. its wavelength is given by the de Broglie relation

$$\lambda = \frac{h}{p} = \frac{6.63 \times 10^{-34} \text{ Js}}{6.4 \times 10^{-22} \frac{\text{kgm}}{\text{s}}} = 1.04 \times 10^{-12} \text{ m}.$$

c. its frequency is given by $f = \frac{c}{\lambda} = \frac{3 \times 10^8 \frac{\text{m}}{\text{s}}}{1.04 \times 10^{-12} \text{ m}} = 2.9 \times 10^{20} \text{ s}^{-1}$.

24.11 A Compton effect experiment

- a. The wavelength and momentum of the incident gamma ray are given as

$$E = \frac{hc}{\lambda} \rightarrow \lambda = \frac{hc}{E} = \frac{(6.63 \times 10^{-34} \text{ Js}) \left(3 \times 10^8 \frac{\text{m}}{\text{s}}\right)}{1.6 \times 10^6 \text{ eV} \times \frac{1.6 \times 10^{-19} \text{ J}}{1 \text{ eV}}} = 7.77 \times 10^{-13} \text{ m and}$$

$$p = \frac{h}{\lambda} = \frac{E}{c} = \frac{6.63 \times 10^{-34} \text{ Js}}{7.77 \times 10^{-13} \text{ m}} = 8.53 \times 10^{-22} \frac{\text{kgm}}{\text{s}} \text{ respectively.}$$

- b. Using the Compton formula for the wavelength of the scattered photon and the fact that the energy is inversely proportional to the wavelength we can write

$$\lambda' = \lambda + \frac{h}{m_e c} (1 - \cos \phi) \rightarrow \frac{\lambda'}{hc} = \frac{\lambda}{hc} + \frac{1}{m_e c^2} (1 - \cos \phi) \rightarrow \frac{1}{E'} = \frac{1}{E} + \frac{(1 - \cos \phi)}{m_e c^2}.$$

- c. The energy of the scattered gamma ray photon is

$$\frac{1}{E'} = \frac{1}{1.6 \text{ MeV}} + \frac{(1 - \cos 50)}{0.511 \text{ MeV}} = 1.324 \text{ MeV}^{-1} \rightarrow E' = 0.755 \text{ MeV} \text{ where the rest mass of the electron is given as}$$

$$m_e c^2 = \left(9.11 \times 10^{-31} \text{ kg} \right) \left(3 \times 10^8 \frac{\text{m}}{\text{s}}\right)^2 \times \frac{1 \text{ eV}}{1.6 \times 10^{-19} \text{ J}} = 0.511 \text{ MeV}.$$

- d. The kinetic energy of the recoiling electron is found using conservation of energy where when the incident gamma ray photon interacts with electrons in the sample, the gamma ray photon loses some energy to the electron as it scatters. Thus the kinetic energy of the recoiling electron is

$$E_{\text{incident}} = E_{\text{scattered}} + KE_{e^-}$$

$$\therefore KE_{e^-} = E_{\text{incident}} - E_{\text{scattered}} = 1.6 \text{ MeV} - 0.755 \text{ MeV} = 0.845 \text{ MeV}$$

- e. The speed of the recoiling electron is given by using the expression for the relativistic kinetic energy. We have

$$KE = 0.845 \text{ MeV} = (\gamma - 1)m_e c^2 = (\gamma - 1)0.511 \text{ MeV}$$

$$\gamma = 1 + \frac{0.845 \text{ MeV}}{0.511 \text{ MeV}} = 1 + 1.654 = 2.654 = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \rightarrow v^2 = 0.858c^2 \rightarrow v = 0.926c$$

24.12 X-rays on a foil target

- a. The energy is given by $E = \frac{hc}{\lambda} = \frac{(6.63 \times 10^{-34} \text{ Js}) \left(3 \times 10^8 \frac{\text{m}}{\text{s}}\right)}{0.012 \times 10^{-9} \text{ m}} = 1.66 \times 10^{-14} \text{ J} = 0.104 \text{ MeV}.$

- b. The scattered wavelength is given by

$$\lambda_f - \lambda_i = \frac{h}{mc} (1 - \cos \phi) = \frac{2h}{mc} = \frac{2(6.63 \times 10^{-34} \text{ Js})}{(9.11 \times 10^{-31} \text{ kg}) \left(3 \times 10^8 \frac{\text{m}}{\text{s}}\right)} = 4.86 \times 10^{-12} \text{ m. Thus,}$$

$$\lambda_f = 4.86 \times 10^{-12} \text{ m} + 1.2 \times 10^{-11} \text{ m} = 1.686 \times 10^{-11} \text{ m. The energy is given by the formula in part a, and is } 1.18 \times 10^{-14} \text{ J} = 0.0741 \text{ MeV.}$$

- c. The energy given to the foil is

$$\Delta E_{\text{foil}} = E_{\text{incident}} - E_{\text{backscattered}} = 0.104 \text{ MeV} - 0.0741 \text{ MeV} = 0.03 \text{ MeV} = 30 \text{ keV}.$$

24.15 To determine the number of photons that strike a screen every second, we divide the total energy per second (1 mW) by the energy per photon. The energy of a photon is given as $E = \frac{hc}{\lambda} = \frac{6.63 \times 10^{-34}\text{ Js} \times 3 \times 10^8 \frac{\text{m}}{\text{s}}}{633 \times 10^{-9}\text{ m}} = 3.14 \times 10^{-19}\text{ J}$. Therefore

the number of photons that strike per second is

$$\frac{\#}{s} = \frac{P}{E_{ph}} = \frac{1 \times 10^{-3} \frac{\text{J}}{\text{s}}}{3.14 \times 10^{-19} \frac{\text{J}}{\text{photon}}} = 3.2 \times 10^{15} \frac{\text{photons}}{\text{s}}.$$

Monday, March 3, 2014

Chapter 24

Questions

24.2 In a photoelectric experiment the intensity refers to the number of photons incident on the metal surface per second. Let a beam of green light with intensity I be incident on the surface and note that it produces a photocurrent. If we switch to blue light of the *same intensity* I , the energy of the individual photons is greater and thus the maximum kinetic energy of the ejected photoelectrons is greater. The intensity is a constant, which is the total energy of the photons in the beam of light. The total energy is a product of the energy of each photon multiplied by the total number of photons. If the energy of each individual photon increases then the number of photons in the beam decreases since we want the total energy of the beam (which is proportional to the intensity) to remain constant. Since the number of photons decreases the number of photoelectrons decreases and the photocurrent decreases.

24.4 If for a particular wavelength of green light we find a stopping potential of -1.5V , this allows us to determine the work function ϕ , or the minimum energy needed to eject a photoelectron. Now, if we switch to a blue light the wavelength is shorter than that of green light and the maximum kinetic energy of the ejected photoelectrons will thus be greater using blue light as opposed to green light.

Multiple-Choice

- 24.2 B
- 24.3 C
- 24.4 D
- 24.6 C

Problems

24.8 Photoelectric effect in cesium

We are given the work function for cesium is $\phi = 2.9\text{ eV} = 4.64 \times 10^{-19}\text{ J}$.

a. The maximum wavelength corresponds to the minimum frequency. Therefore,

$$KE_{\min} = hf_{\min} - \phi = 0 \text{ which gives } f_{\min} = \frac{\phi}{h} = \frac{4.64 \times 10^{-19}\text{ J}}{6.63 \times 10^{-34}\text{ Js}} = 7.0 \times 10^{14}\text{ s}^{-1}. \text{ From}$$

$$c = f_{\min} \lambda_{\max} \rightarrow \lambda_{\max} = \frac{c}{f_{\min}} = \frac{3 \times 10^8 \frac{\text{m}}{\text{s}}}{7.0 \times 10^{14}\text{ s}^{-1}} = 4.28 \times 10^{-7}\text{ m} = 428\text{ nm}.$$

- b. If 400nm photons are used, their energy is given by

$$E = \frac{hc}{\lambda} = \frac{6.63 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \frac{\text{m}}{\text{s}}}{400 \times 10^{-9} \text{ m}} = 4.97 \times 10^{-19} \text{ J} \times \frac{1\text{eV}}{1.6 \times 10^{-19} \text{ J}} = 3.11\text{eV}.$$

Therefore the maximum kinetic energy is given as

$$KE_{\text{max}} = hf - \phi = 3.11\text{eV} - 2.9\text{eV} = 0.21\text{eV} \times \frac{1.6 \times 10^{-19} \text{ J}}{1\text{eV}} = 3.33 \times 10^{-20} \text{ J}.$$

- c. A 1 W beam of photons corresponds to 1 J of photons incident per second. In 1 J of photons there are $\frac{1\text{J}}{4.97 \times 10^{-19} \frac{\text{J}}{\text{photon}}} = 2.01 \times 10^{18}$ photons. If the photo ejection

of an electron is 100% efficient, then for each photon lost, one electron is produced. Thus the photocurrent is the amount of charge produced each second, where 1 electron has $1.6 \times 10^{-19} \text{ C}$ of charge. This corresponds to a total charge of $Q = 2.01 \times 10^{18} \times 1.6 \times 10^{-19} \text{ C} = 0.322 \text{ C}$ of charge in 1 second . Therefore the photocurrent is $0.322 \text{ A} = 322 \text{ mA}$.

- d. If green photons are used with a wavelength of 500 nm , this corresponds to an energy of

$$E = \frac{hc}{\lambda} = \frac{6.63 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \frac{\text{m}}{\text{s}}}{500 \times 10^{-9} \text{ m}} = 3.98 \times 10^{-19} \text{ J} \times \frac{1\text{eV}}{1.6 \times 10^{-19} \text{ J}} = 2.49\text{eV}.$$

The maximum f that will allow for photo ejection of electrons is the one where the electrons are ejected with a maximum kinetic energy equal to zero. Therefore

$$KE_{\text{min}} = hf_{\text{min}} - \phi = 0, \text{ and solving for } \phi \text{ we obtain } hf_{\text{min}} = \phi = 2.49\text{eV}.$$

- 24.9 The maximum KE is given by the product of the stopping potential (0.82V) and the electron's charge (e^-). Thus the maximum $KE = eV_{\text{stop}} = 0.82\text{eV}$. This is equal to the energy of the photons incident minus the work function (the minimum energy needed to eject a photoelectron). In symbols,

$$KE_{\text{max}} = hf - \phi = \frac{hc}{\lambda} - \phi$$

$$\rightarrow 0.82\text{eV} = \left(\frac{6.63 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \frac{\text{m}}{\text{s}}}{400 \times 10^{-9} \text{ m}} \right) \times \frac{1\text{eV}}{1.6 \times 10^{-19} \text{ J}} - \phi \rightarrow \phi = 2.29\text{eV}$$

24.10 A photoelectric effect experiment

- a. The maximum kinetic energy is given by

$$KE_{\text{max}} = hf - \phi = \frac{hc}{\lambda} - \phi$$

$$KE_{\text{max}} = \left(\frac{6.63 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \frac{\text{m}}{\text{s}}}{410 \times 10^{-9} \text{ m}} \right) \times \frac{1\text{eV}}{1.6 \times 10^{-19} \text{ J}} - 2.28\text{eV}$$

$$KE_{\text{max}} = 3.03\text{eV} - 2.28\text{eV} = 0.75\text{eV}$$

In order to calculate the speed, we use the expression for the relativistic kinetic energy. We have

$$KE = 0.75eV = (\gamma - 1)m_e c^2 = (\gamma - 1)0.511MeV$$

$$\gamma = 1 + \frac{0.75eV}{0.511 \times 10^6 eV} = 1 + 0000015 = 1.0000015$$

$$\text{and the speed is therefore } \gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \rightarrow v^2 = 2.94 \times 10^{-6} c^2 \rightarrow v = 0.0017c$$

- b. Based on the speed calculated in *part a*, the electron is not relativistic.
 c. The minimum frequency corresponds to an electron ejected with a kinetic energy equal to zero. Therefore, $KE_{\min} = hf_{\min} - \phi = 0$ which gives

$$f_{\min} = \frac{\phi}{h} = \frac{2.28eV \times \frac{1.6 \times 10^{-19} J}{1eV}}{6.63 \times 10^{-34} Js} = 5.5 \times 10^{14} s^{-1}.$$

- d. The minimum frequency corresponds to the maximum wavelength. Therefore we

$$\text{have } c = f_{\min} \lambda_{\max} \rightarrow \lambda_{\max} = \frac{c}{f_{\min}} = \frac{3 \times 10^8 \frac{m}{s}}{5.5 \times 10^{14} s^{-1}} = 5.45 \times 10^{-7} m = 545nm.$$

- e. For $700nm$ photons we have the maximum kinetic energy given as

$$KE_{\max} = hf - \phi = \frac{hc}{\lambda} - \phi$$

$$KE_{\max} = \left(\frac{6.63 \times 10^{-34} Js \times 3 \times 10^8 \frac{m}{s}}{700 \times 10^{-9} m} \right) \times \frac{1eV}{1.6 \times 10^{-19} J} - 2.28eV$$

$$KE_{\max} = 1.78eV - 2.28eV = -0.50eV$$

Or, we have that no photoelectrons are produced. In addition we know that the maximum wavelength for photo production is $545nm$, and we are well beyond this, so no photocurrent would be produced.