Name_____ Physics 120 Quiz #2, January 20, 2012

Please show all work, thoughts and/or reasoning in order to receive partial credit. The quiz is worth 10 points total.

- 1. The x-component of a particle's velocity is sampled every 5 seconds. The data are fit with a straight line as shown in the figure to the right. Assuming the fit is a good approximation to the motion, which of the following best represents the x-component of the force on the particle as a function of time? a. $0 + \frac{1}{1 + 1} + \frac{1}$
- 2. A ball of mass m = 50g is thrown at the floor with a velocity $\vec{v}_i = \langle 4, -5, 0 \rangle \frac{m}{s}$. It rebounds from the floor with a velocity of $\vec{v}_f = \langle 4, 5, 0 \rangle \frac{m}{s}$ and is in contact with the floor for a time of $1.5 \times 10^{-3} s$.
 - a. What is the force that the *ball exerts on the floor*?

$$\vec{p}_{f} = \vec{p}_{i} + \vec{F}_{net}\Delta t \Rightarrow \frac{\vec{p}_{f} - \vec{p}_{i}}{\Delta t} = \vec{F}_{\text{floor on ball}}$$

$$\frac{0.05kg \times \left(\langle 4, 5, 0 \rangle \frac{m}{s} - \langle 4, -5, 0 \rangle \frac{m}{s}\right)}{1.5 \times 10^{-3} s} = \langle 0, 333, 0 \rangle N = \vec{F}_{\text{floor on ball}}$$

$$\vec{F}_{\text{ball on floor}} = -\vec{F}_{\text{floor on ball}} = \langle 0, -333, 0 \rangle N$$

b. After the ball loses contact with the floor it is subjected to a constant force due to gravity given by $\vec{F}_{net} = \langle 0, -0.49, 0 \rangle N$. How high does the ball rise above the floor, taken to be at y = 0?

$$p_{fy} = p_{iy} + F_{net,y} \Delta t_{rise} \Rightarrow 0 = mv_{iy} + F_{net,y} \Delta t_{rise} = 0.25 \frac{m}{s} - 0.49 \frac{m}{s^2} \Delta t_{rise} \Rightarrow \Delta t_{rise} = 0.51s$$

$$y_y = y_i + v_{avg,y} \Delta t_{rise} = y_i + \left[\frac{v_{i,y} + v_{f,y}}{2}\right] \Delta t_{rise} = 0m + \left[\frac{5\frac{m}{s} + 0\frac{m}{s}}{2}\right] \times 0.51s = 1.3m$$

Useful formulas:

$$\vec{p} = \gamma m \vec{v}$$
 $k_{eff, parallel} = n_{parallel} k_{individual}$
 $\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$
 $k_{eff, series} = \frac{k_{individual}}{n_{series}}$
 $\vec{v}_{avg} = \frac{\vec{v}_i + \vec{v}_f}{2}$
 $stress = Ystrain \rightarrow \frac{F}{A} = Y \frac{\Delta L}{L}$
 $\vec{F}_g = m \vec{g}$
 $\vec{F}_{gravity} = \frac{GM_1M_2}{r_1^2} \hat{r}_{12}$
 $\vec{F}_{spring} = -k\vec{s}; \quad \vec{s} = (L - L_o)\hat{s}$
 $W = \int \vec{F} \cdot d\vec{r} = \Delta KE = -\Delta U$
 $U_g = mgy$
 $U_s = \frac{1}{2}ks^2$
 $KE = (\gamma - 1)mc^2$

Momentum Principle:

$$\vec{p}_{f} = \vec{p}_{i} + \vec{F}_{net}\Delta t; \quad \Delta t = \text{large}$$

$$\vec{p}_{f} = \vec{p}_{i} + \vec{F}_{net}dt; \quad dt = \frac{\Delta t}{n} = \text{small}$$
Position-update:

$$\vec{r}_{f} = \vec{r}_{i} + \vec{v}_{avg}\Delta t = \vec{r}_{i} + \frac{\vec{p}}{m\sqrt{1 + \frac{p^{2}}{m^{2}c^{2}}}}\Delta t; \quad \Delta t = \text{large}$$

$$\vec{r}_{f} = \vec{r}_{i} + \vec{v}_{f}dt; \quad dt = \frac{\Delta t}{n} = \text{small}$$

$$\Delta E = W = \Delta U_{g} + \Delta U_{s} + \Delta KE$$

Energy principle: Geometry /Algebra Circles Triangles Spheres $C = 2\pi r$ $A = \frac{1}{2}bh$ $A = 4\pi r^2$ $A = \pi r^2$ $V = \frac{4}{3}\pi r^3$ Quadratic equation : $ax^2 + bx + c = 0$, whose solutions are given by : $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Vectors

magnitude of a vector:
$$|\vec{a}| = \sqrt{a_x^2 + a_y^2 + a_z^2}$$

writing a vector: $\vec{a} = \langle a_x, a_y, a_z \rangle = |\vec{a}|\hat{a} = a_x\hat{i} + a_y\hat{j} + a_z\hat{k}$

Useful Constants

$$g = 9.8 \frac{m}{r^2}$$

 $G = 6.67 \times 10^{-11} \frac{Nm^2}{kg^2}$
 $le = 1.6 \times 10^{-19} C$
 $k = \frac{1}{4\pi\epsilon_o} = 9 \times 10^9 \frac{C^2}{Nm^2}$
 $\epsilon_o = 8.85 \times 10^{-12} \frac{Nm^2}{C^2}$
 $leV = 1.6 \times 10^{-19} J$
 $\mu_o = 4\pi \times 10^{-7} \frac{Tm}{A}$
 $c = 3 \times 10^8 \frac{m}{s}$
 $h = 6.63 \times 10^{-34} Js$
 $m_e = 9.11 \times 10^{-31} kg = \frac{0.511 MeV}{c^2}$
 $m_p = 1.67 \times 10^{-27} kg = \frac{937.1 MeV}{c^2}$
 $m_n = 1.69 \times 10^{-27} kg = \frac{948.3 MeV}{c^2}$
 $lamu = 1.66 \times 10^{-27} kg = \frac{931.5 MeV}{c^2}$
 $N_A = 6.02 \times 10^{23}$
 $Ax^2 + Bx + C = 0 \Rightarrow x = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$