Name_____ Physics 120 Quiz #4, February 10, 2012

Please show all work, thoughts and/or reasoning in order to receive partial credit. The quiz is worth 10 points total.

1. A person hoists a bucket of water from a well and holds the rope, keeping the bucket at rest as in the left photo. Call this situation *A*. A short time later the person ties the rope to the bucket so that the rope holds the bucket in place as in the right photo. Call this situation *B*.



- a. The tension in situation *B* is greater than in situation *A*.
- b. The tension in situation *B* is equal to that in situation *A*.
- c. The tension in situation *B* is less than that in situation *A*.
- d. Three is no way that the individual tensions in the ropes can be determined.
- 2. A Boeing 737-600 jet prepares to takeoff from a runway. The engines provide constant forward thrust given by $\vec{F}_{thrust} = \langle 173400,0,0 \rangle N$ and while the plane moves down the runway friction due to the rubber tires and the concrete runway (with coefficient of kinetic friction given by $\mu_k = 0.2$) opposes the motion of the jet. (All data are obtained from www.boeing.com/commercial/737family/pf/pf_600tech.html)
 - a. What is the expression for the net force vector?

$$\vec{F}_{net} = \left\langle F_{thrust} - F_{friction}, F_{normal} - F_{weight}, 0 \right\rangle$$

b. Starting from a fundamental principle, if the plane starts from rest and takes off when its velocity is $\vec{v}_f = \langle 77, 0, 0 \rangle \frac{m}{s}$ and not before, what is the mass of the Boeing 737-600 if the jet takes 60s to get to from rest to this final velocity?

$$\begin{split} F_{net} &= \frac{dp}{dt} \rightarrow = \left\langle F_{thrust} - F_{friction}, F_{normal} - F_{weight}, 0 \right\rangle = \left\langle m \frac{dv_x}{dt}, 0, 0 \right\rangle \\ mv_{fx} - mv_{ix} &= m \int_{v_{ix}}^{v_{fx}} dv = \left(F_{thrust} - F_{friction} \right) \int_{t_i}^{t_f} dt = \left(F_{thrust} - \mu F_{normal} \right) \Delta t = \left(F_{thrust} - \mu mg \right) \Delta t \\ m \left(v_{fx} + \mu g \Delta t \right) = F_{thrust} \Delta t \Rightarrow m = \frac{F_{thrust} \Delta t}{v_{fx} + \mu g \Delta t} = \frac{173400N \times 60s}{77 \frac{m}{s} + \left(0.2 \times 9.8 \frac{m}{c^2} \times 60s \right)} = 53464 kg \end{split}$$

c. How far down the runway does the plane takeoff?

$$\vec{v} = \frac{d\vec{r}}{dt} \Rightarrow dx = v_{fx}dt \Rightarrow \Delta x = \int_{x_i}^{x_f} dx = \int_{t_i}^{t_f} \left(\frac{(F_{thrust} - \mu mg)t}{m}\right) dt = \frac{1}{2} \left(\frac{F_{thrust} - \mu mg}{m}\right) t^2$$
$$\Delta x = \frac{1}{2} \times \left(\frac{173400N - \left(0.2 \times 53464kg \times 9.8\frac{m}{s^2}\right)}{53464kg}\right) (60s)^2 = 2310m$$

Useful formulas:

$$\vec{p} = \gamma m \vec{v}$$
 $k_{eff, parallel} = n_{parallel} k_{individual}$

 $\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$
 $k_{eff, series} = \frac{k_{individual}}{n_{series}}$

 $\vec{v}_{avg} = \frac{\vec{v}_i + \vec{v}_f}{2}$
 $stress = Ystrain \rightarrow \frac{F}{A} = Y$

 $\vec{F}_g = m \vec{g}$
 $v_s = \sqrt{\frac{k_{IAB}}{m_{atom}}} d$

 $F_{fr} = \mu F_N$

 $\vec{F}_{gravity} = \frac{GM_1M_2}{r_{12}^2} \hat{r}_{12}$
 $k_{IAB} = Yd$

 $\vec{F}_{spring} = -k \vec{s}; \quad \vec{s} = (L - L_o) \hat{s}$

 $W = \int \vec{F} \cdot d\vec{r} = \Delta KE = -\Delta U$

 $U_g = -\frac{GM_1M_2}{r}$

 $U_g = mgy$

 $U_s = \frac{1}{2}ks^2$

 $KE = (\gamma - 1)mc^2$

 $\frac{\Delta L}{L}$

Useful Constants

$$g = 9.8 \frac{m}{s^{2}}$$

$$G = 6.67 \times 10^{-11} \frac{Nm^{2}}{kg^{2}}$$

$$le = 1.6 \times 10^{-19} C$$

$$k = \frac{1}{4\pi\epsilon_{o}} = 9 \times 10^{9} \frac{c^{2}}{Nm^{2}}$$

$$\epsilon_{o} = 8.85 \times 10^{-12} \frac{Nm^{2}}{C^{2}}$$

$$leV = 1.6 \times 10^{-19} J$$

$$\mu_{o} = 4\pi \times 10^{-7} \frac{Tm}{A}$$

$$c = 3 \times 10^{8} \frac{m}{s}$$

$$h = 6.63 \times 10^{-34} Js$$

$$m_{e} = 9.11 \times 10^{-31} kg = \frac{0.511MeV}{c^{2}}$$

$$m_{p} = 1.67 \times 10^{-27} kg = \frac{937.1MeV}{c^{2}}$$

$$m_{n} = 1.69 \times 10^{-27} kg = \frac{948.3MeV}{c^{2}}$$

$$lamu = 1.66 \times 10^{-27} kg = \frac{931.5MeV}{c^{2}}$$

$$N_{A} = 6.02 \times 10^{23}$$

$$Ax^{2} + Bx + C = 0 \Rightarrow x = \frac{-B \pm \sqrt{B^{2} - 4AC}}{2A}$$

 $\vec{p}_{f} = \vec{p}_{i} + \vec{F}_{net}\Delta t; \quad \Delta t = \text{large}$ Momentum Principle: $\vec{p}_{f} = \vec{p}_{i} + \vec{F}_{net}dt; \quad dt = \frac{\Delta t}{n} = \text{small}$ Position-update: $\vec{r}_{f} = \vec{r}_{i} + \vec{v}_{avg}\Delta t = \vec{r}_{i} + \frac{\vec{p}}{m\sqrt{1 + \frac{p^{2}}{m^{2}c^{2}}}}\Delta t; \quad \Delta t = \text{large}$ $\vec{r}_{f} = \vec{r}_{i} + \vec{v}_{f}dt; \quad dt = \frac{\Delta t}{n} = \text{small}$ $\Delta E = W = \Delta U_{g} + \Delta U_{s} + \Delta KE$

Energy principle: Geometry /Algebra Circles Triangles Spheres $C = 2\pi r$ $A = \frac{1}{2}bh$ $A = 4\pi r^2$ $A = \pi r^2$ $V = \frac{4}{3}\pi r^3$ Quadratic equation : $ax^2 + bx + c = 0$,

whose solutions are given by :
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Vectors

$$\begin{split} \text{magnitude of } a \;\; \text{vector}: |\vec{a}| &= \sqrt{a_x^2 + a_y^2 + a_z^2} \\ \text{writing } a \;\; \text{vector}: \;\; \vec{a} &= \left\langle a_x, a_y, a_z \right\rangle = |\vec{a}|\hat{a} = a_x \hat{i} + a_y \hat{j} + a_z \hat{k} \end{split}$$