Name
Physics 120 Quiz \#4, February 10, 2012
Please show all work, thoughts and/or reasoning in order to receive partial credit. The quiz is worth 10 points total.

1. A person hoists a bucket of water from a well and holds the rope, keeping the bucket at rest as in the left photo. Call this situation $A$. A short time later the person ties the rope to the bucket so that the rope holds the bucket in place as in the right photo. Call this situation $B$.

a. The tension in situation $B$ is greater than in situation $A$.
b. The tension in situation $B$ is equal to that in situation $A$.
c. The tension in situation $B$ is less than that in situation $A$.
d. Three is no way that the individual tensions in the ropes can be determined.
2. A Boeing 737-600 jet prepares to takeoff from a runway. The engines provide constant forward thrust given by $\vec{F}_{\text {thrust }}=\langle 173400,0,0\rangle N$ and while the plane moves down the runway friction due to the rubber tires and the concrete runway (with coefficient of kinetic friction given by $\mu_{k}=0.2$ ) opposes the motion of the jet. (All data are obtained from www.boeing.com/commercial/737family/pf/pf_600tech.html)
a. What is the expression for the net force vector?

$$
\vec{F}_{\text {net }}=\left\langle F_{\text {thrust }}-F_{\text {friction }}, F_{\text {normal }}-F_{\text {weight }}, 0\right\rangle
$$

b. Starting from a fundamental principle, if the plane starts from rest and takes off when its velocity is $\vec{v}_{f}=\langle 77,0,0\rangle \frac{m}{s}$ and not before, what is the mass of the Boeing 737-600 if the jet takes 60 s to get to from rest to this final velocity?

$$
\begin{aligned}
& F_{\text {net }}=\frac{d p}{d t} \rightarrow=\left\langle F_{\text {thrust }}-F_{\text {friction }}, F_{\text {normal }}-F_{\text {weight }}, 0\right\rangle=\left\langle m \frac{d v_{x}}{d t}, 0,0\right\rangle \\
& m v_{f x}-m v_{i x}=m \int_{v_{\text {it }}}^{v_{\text {ft }}} d v=\left(F_{\text {thrust }}-F_{\text {friction }}\right) \int_{t_{i}}^{t_{f}} d t=\left(F_{\text {thrust }}-\mu F_{\text {normal }}\right) \Delta t=\left(F_{\text {thrust }}-\mu \mathrm{mg}\right) \Delta t \\
& m\left(v_{f x}+\mu g \Delta t\right)=F_{\text {thrust }} \Delta t \Rightarrow m=\frac{F_{\text {thrust }} \Delta t}{v_{f x}+\mu g \Delta t}=\frac{173400 \mathrm{~N} \times 60 \mathrm{~s}}{77 \frac{\mathrm{~m}}{\mathrm{~s}}+\left(0.2 \times 9.8 \frac{\mathrm{~m}}{\mathrm{~s}^{2}} \times 60 \mathrm{~s}\right)}=53464 \mathrm{~kg}
\end{aligned}
$$

c. How far down the runway does the plane takeoff?

$$
\begin{aligned}
& \vec{v}=\frac{d \vec{r}}{d t} \Rightarrow d x=v_{f x} d t \Rightarrow \Delta x=\int_{x_{i}}^{x_{f}} d x=\int_{t_{i}}^{t_{f}}\left(\frac{\left(F_{\text {thrust }}-\mu m g\right) t}{m}\right) d t=\frac{1}{2}\left(\frac{F_{\text {thrust }}-\mu m g}{m}\right) t^{2} \\
& \Delta x=\frac{1}{2} \times\left(\frac{173400 N-\left(0.2 \times 53464 \mathrm{~kg} \times 9.8 \frac{\mathrm{~m}}{s^{2}}\right)}{53464 \mathrm{~kg}}\right)(60 \mathrm{~s})^{2}=2310 \mathrm{~m}
\end{aligned}
$$

Useful formulas:

$$
\vec{p}=\gamma m \vec{v} \quad k_{\text {eff ,parallel }}=n_{\text {parallel }} k_{\text {individual }}
$$

$\gamma=\frac{1}{\sqrt{v^{2}}}$

$$
k_{\text {eff, ,series }}=\frac{k_{\text {individual }}}{n_{\text {series }}}
$$

$\vec{v}_{\text {avg }}=\frac{\vec{v}_{i}+\vec{v}_{f}}{2} \quad$ stress $=$ Ystrain $\rightarrow \frac{F}{A}=Y \frac{\Delta L}{L}$
$\vec{F}_{g}=m \vec{g}$

$$
v_{s}=\sqrt{\frac{k_{I A B}}{m_{\text {atom }}}} d
$$

$F_{f r}=\mu F_{N}$
$\vec{F}_{\text {gravity }}=\frac{G M_{1} M_{2}}{r_{12}^{2}} \hat{r}_{12} \quad k_{I A B}=Y d$
$\vec{F}_{\text {spring }}=-k \vec{s} ; \quad \vec{s}=\left(L-L_{o}\right) \hat{s}$
$W=\int \vec{F} \cdot d \vec{r}=\Delta K E=-\Delta U$
$U_{g}=-\frac{G M_{1} M_{2}}{r}$
$U_{g}=m g y$
$U_{s}=\frac{1}{2} k s^{2}$
$K E=\frac{1}{2} m v^{2}$
$K E=(\gamma-1) m c^{2}$

Momentum Principle
$\vec{p}_{f}=\vec{p}_{i}+\vec{F}_{n e t} \Delta t ; \quad \Delta t=$ large
Useful Constants
$g=9.8 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}$
$G=6.67 \times 10^{-11} \frac{\mathrm{Nm}^{2}}{\mathrm{~kg}^{2}}$
$1 e=1.6 \times 10^{-19} \mathrm{C}$
$k=\frac{1}{4 \pi \varepsilon_{o}}=9 \times 10^{9} \frac{\mathrm{C}^{2}}{\mathrm{Nm}^{2}}$
$\varepsilon_{o}=8.85 \times 10^{-12} \frac{\mathrm{Nm}{ }^{2}}{\mathrm{C}^{2}}$
$1 \mathrm{eV}=1.6 \times 10^{-19} \mathrm{~J}$
$\mu_{o}=4 \pi \times 10^{-7} \frac{\mathrm{Tm}}{\mathrm{A}}$
$c=3 \times 10^{8} \frac{\mathrm{~m}}{\mathrm{~s}}$
$h=6.63 \times 10^{-34} \mathrm{~J} S$
Energy principle:
Geometry /Algebra
Circles Triangles Spheres
$C=2 \pi r \quad A=\frac{1}{2} b h \quad A=4 \pi r^{2}$
$A=\pi r^{2} \quad V=\frac{4}{3} \pi r^{3}$
Quadratic equation : $a x^{2}+b x+c=0$,
whose solutions are given by : $x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Vectors
magnitude of a vector: $|\vec{a}|=\sqrt{a_{x}^{2}+a_{y}^{2}+a_{z}^{2}}$
writing a vector: $\quad \vec{a}=\left\langle a_{x}, a_{y}, a_{z}\right\rangle=|\vec{a}| \hat{a}=a_{x} \hat{i}+a_{y} \hat{j}+a_{z} \hat{k}$
$m_{p}=1.67 \times 10^{-27} k g=\frac{937.1 \mathrm{MeV}}{c^{2}}$
$m_{n}=1.69 \times 10^{-27} \mathrm{~kg}=\frac{948.3 \mathrm{MeV}}{c^{2}}$
$1 \mathrm{amu}=1.66 \times 10^{-27} \mathrm{~kg}=\frac{931.5 \mathrm{MeV}}{\mathrm{c}^{2}}$
$N_{A}=6.02 \times 10^{23}$
$A x^{2}+B x+C=0 \rightarrow x=\frac{-B \pm \sqrt{B^{2}-4 A C}}{2 A}$

