

## The Extended IS-LM Model

with risk premia and nominal versus real interest rates

*Based on Blanchard, 7<sup>th</sup> edition, chapter 6*

### The Fisher Equation

$$r_t = i_t - \pi_{t+1}^e \Leftrightarrow i_t = r_t + \pi_{t+1}^e.$$

### Risk and Risk Premia

Let  $i$  be the nominal interest rate on a riskless bond, and  $i + x$  be the nominal interest rate on a risky bond, which is a bond which has probability  $p$  of defaulting. Call  $x$  the risk premium. Then, to get the same expected return on the risky bonds as on the riskless bond, the following relation must hold:

$$(1+i) = (1-p)(1+i+x) + p(0).$$

Reorganizing the above gives:

$$x = \frac{(1+i)p}{(1-p)}.$$

An example: Let  $i = 3\%$ , and  $p = 5\%$ , then from the above formula we get,  $x = 5.42\%$ .

### Extending the IS-LM

IS relation:

$$Y = C(Y - T) + I(Y, i - \pi^e + x) + G + NX.$$

LM relation:  $i = \bar{i}$ .

However, “although the central bank formally chooses the nominal interest rate, it can choose it in such a way as to achieve the real interest rate it wants”. (This ignores the issue of zero lower bound—to be discussed.)

