1. The speed of the tip of the minute hand on a town clock is 1.75 mm/s.
   a. What is the speed of the second hand if it has the same length?
   b. What is the centripetal acceleration of the tip of the second hand?

   a. For the minute hand, it takes 3600s per revolution.
   
   Thus, \( v = \frac{2\pi r}{T} \rightarrow r = \frac{vT}{2\pi} = \frac{\left(1.75 \times 10^{-3}\ \text{m/s}\right)(3600\text{s})}{2\pi} = 1.0\text{m} \). Therefore for the second hand which makes 60s per revolution, the velocity is given as
   \( v = \frac{2\pi r}{60\text{s}} = \frac{2\pi(1.0\text{m})}{60\text{s}} = 0.105\ \text{m/s} \).

   b. \( a = \frac{v^2}{r} = \frac{(0.105\ \text{m/s})^2}{1.0\text{m}} = 0.011\ \text{m/s}^2 \).

2. Consider a conical pendulum with an 80kg bob on a 10m long wire making an angle of 5° with respect to the vertical as shown below.
   a. What are the horizontal and vertical components of the force exerted by the wire on the pendulum?
   b. What is the radial acceleration of the bob?

   a. From the free body diagram
   \[
   \sum F_x : \quad F_x = F_T \sin 5 = \frac{mv^2}{R} \tag{1}
   \]
   \[
   \sum F_y : \quad F_y = F_T \cos 5 - mg = 0 \tag{2}
   \]

   b. From (2) we solve for the tension force and substitute into (1). Dividing by the mass we get for the radial acceleration, 0.857 m/s².

3. A 4300lb truck passes over a bump in a road that follows the arc of a circle of radius 42m.
   a. What force does the road exert on the car as the car passes the highest point of the bump if the car is traveling at 16 m/s?
   b. What is the maximum speed that the car can have as it passes this highest point before losing contact with the road?

   a. 4300 lb converts to 1954.6kg. From the free body diagram below, \( \sum F_y : \quad F_N - mg = -\frac{mv^2}{R} \rightarrow F_N = mg - \frac{mv^2}{R} = 7241.3\text{N} \).
b. The maximum speed is when the car leaves the road, thus in part a, we set the normal force equal to zero. This gives for the maximum speed
\[ v = \sqrt{Rg} = \sqrt{42m \times 9.8 \frac{m}{s^2}} = 20.3 \frac{m}{s}. \]

4. In one model of a hydrogen atom, the electron in orbit around the proton experiences an attractive force of about \( 8.2 \times 10^{-8} \) N. If the radius of the orbit is \( 5.3 \times 10^{-11} \) m, how many revolutions does the electron make each second? This is called the frequency of the orbit.

\[
F = m \frac{v^2}{r}, \quad \text{which gives} \quad v = \sqrt{\frac{Fr}{m}} = \sqrt{\frac{(5.30 \times 10^{-11} \text{ m})(8.20 \times 10^{-8} \text{ N})}{9.11 \times 10^{-31} \text{ kg}}} = 2.18 \times 10^6 \text{ m/s}
\]

frequency = \( (2.18 \times 10^6 \text{ m/s}) \left[ \frac{1 \text{ rev}}{2\pi(5.30 \times 10^{-11} \text{ m})} \right] = 6.56 \times 10^{15} \text{ rev/s} \)

5. An air puck of mass 0.250 kg is tied to a string and allowed to revolve in a circle of radius 1.00 m on a frictionless horizontal table as shown below. The other end of the string passes through a hole in the center of the table and a mass of 1.00 kg is attached to it. The suspended mass remains in equilibrium while the puck on the tabletop revolves.

a. What is the tension in the string?

(b) The centripetal force is provided by the tension in the string. Hence,
\[ F_c = T = 9.80 \text{ N} \]
(c) Using \( F_r = \frac{m_{puck}v^2}{r} \), we have \( v = \sqrt{\frac{rF_r}{m_{puck}}} = \sqrt{\frac{(1.00)(9.80)}{0.250}} = 6.26 \text{ m/s} \)

6. A child’s toy consists of a small wedge that has an acute angle \( \theta \). The sloping side of the wedge is frictionless, and a mass \( m_a \) on it remains at constant height if the wedge is spun at a certain speed as shown below. The wedge is spun by rotating a vertical rod that is firmly attached to the wedge at the bottom end. Show that, when the mass sits a distance \( L \) up along the sloping side, the speed of the mass is \( v = \sqrt{gL \sin \theta} \).

\[
\sum F_x : \quad F_N \sin \theta = \frac{m v^2}{x} \quad (1)
\]
\[
\sum F_y : \quad F_N \cos \theta - mg = 0 \quad (2)
\]

From (2) we get the normal force, \( F_N = \frac{mg}{\cos \theta} \). Substituting this into (1) we get that \( v^2 = gl \cos \theta \tan \theta \) where \( x = L \cos \theta \). Thus taking the square root produces the desired result.

7. An amusement park ride consists of a rotating circular platform 8.0m in diameter from which 10kg seats are suspended at the end of 2.5m massless chains as shown below. When the system rotates the chains make an angle of \( \theta = 28^\circ \) with respect to the vertical.

a. What is the speed of each seat?
b. What does the free body diagram look like for a 40kg child riding in the seat?
c. What is the tension in the chain?
d. What is the speed of the chair with the child in it?
e. How would parts a – d change if the chains were not massless, but each had a mass of 4kg?

a. From the free body diagram,
\[ \sum F_y : F_T \sin \theta = \frac{mv^2}{R} \quad (1) \]
\[ \sum F_x : F_T \cos \theta - m_{\text{seat}} g = 0 \quad (2) \]

From (2) we get the tension force and substituting this into (1) we find
\[ v_{\text{seat}} = \sqrt{gR \tan \theta} = \sqrt{g(R_{\text{ride}} + l) \tan \theta} = \sqrt{g(R_{\text{ride}} + 2.5 \sin \theta) \tan \theta} = 5.19 \text{ m/s}. \]

b. See drawing above.

c. If the 28° angle is constant, then adding a rider creates a tension force given by
\[ F_T \cos \theta - m_{\text{seat}} g - m_{\text{rider}} g = 0 \rightarrow F_T = \frac{(10\text{ kg} + 40\text{ kg}) \cdot 9.8 \text{ m/s}^2}{\cos 28} = 555 \text{ N} \]

d. If the chains have mass then the tension force is all that changes, since the machine’s motor can spin presumably at a rate that keeps the angle constant. Thus
\[ F_T \cos \theta - m_{\text{seat}} g - m_{\text{rider}} g - 2m_{\text{chains}} g = 0 \rightarrow F_T = \frac{(10\text{ kg} + 40\text{ kg} + 2 \times 4\text{ kg}) \cdot 9.8 \text{ m/s}^2}{\cos 28} = 643.8 \text{ N} \]

8. A model airplane of mass 0.750 kg flies in a horizontal circle at the end of a 60 m control wire, with a speed of 35 m/s. What is the tension in the wire if the plane makes a constant angle of 20° with the horizontal? The forces exerted on the plane are the pull of the control wire, the weight of the plane and the aerodynamic lift, which acts at 20° inward from the vertical as shown below.

\[ \sum F_y : F_L \cos 20 - mg - F_T \sin 20 = 0 \quad (1) \]
\[ \sum F_x : F_T \cos 20 + F_L \sin 20 = \frac{mv^2}{R} \quad (2) \]

From (1) we get the lifting force: \( F_L = \frac{F_T \sin 20 + mg}{\cos 20} \) and substituting this into (2) we find that the tension force is given as 12.8 N.