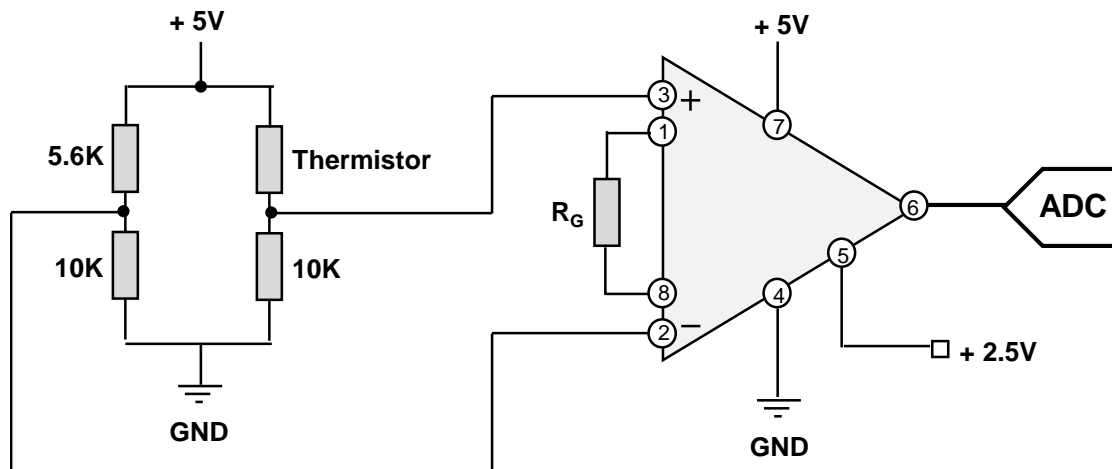


## HW 2 – Temperature Measurement Systems

### (12 problems for 100 pts)

### Thermistor Circuit Design

You are asked to design a system to measure temperature from 30 °C up to 50°C. Consider the signal conditioning electronics shown in the figure. At  $T = 30^\circ\text{C}$ , the thermistor resistance is  $R_T = 8.06 \text{ kohm}$  and the tempco is  $\alpha = -4.25\%/^\circ\text{C}$ . At  $T = 50^\circ\text{C}$ , the thermistor has  $R_{TH} = 3.61 \text{ kohm}$  and  $\alpha = -3.8\%/^\circ\text{C}$ . The instrumentation amplifier is powered by +5 V and GND with an offset voltage of 2.5V. The amplifier output is fed to an 8-bit ADC operating from 0 to 5V.



- PROBLEM 1:** Derive the equation for  $V_{MEAS}$  (the output of the instrumentation amplifier).
- PROBLEM 2:** Most instrumentation amplifiers have a limited output voltage range. If an amplifier is powered by  $+V_S$  and GND, the highest output is typically  $V_S - 1$  while the lowest output is typically 1V. For example, an amplifier powered by +9V and GND has a maximum output of 8V and a minimum output of 1V. For this problem, you must choose between an amplifier gain of 1, 1.5, 2, 2.5, 3, 3.5, 4. Which is the best choice? Show all work!

Hint #1: Think about whether your maximum signal is limited by the amplifier or the ADC.

Hint #2: You should get  $A_d = 3$ .

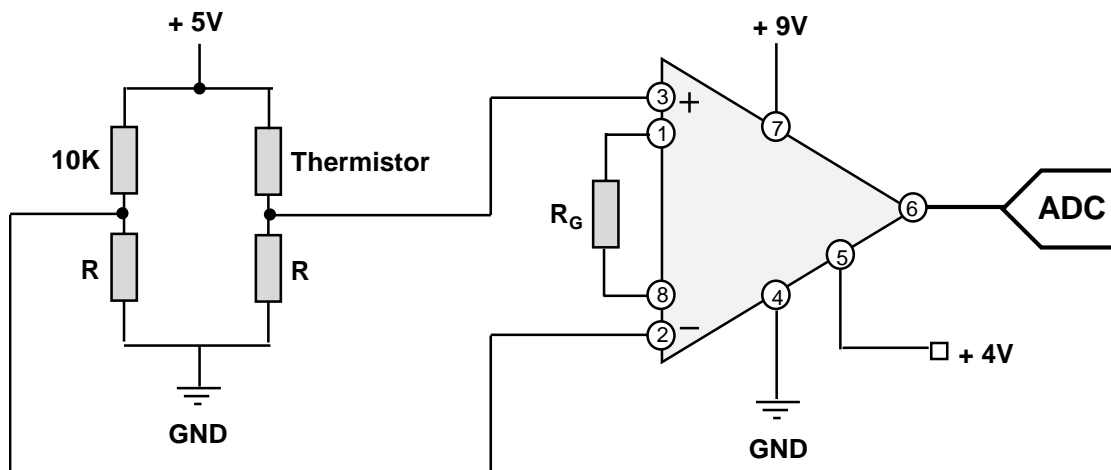
- PROBLEM 3:** Suppose the output of the instrumentation amplifier has a noise voltage of  $4 \text{ mV}_{RMS}$ . What is the temperature sensitivity at  $T = 50^\circ\text{C}$ ? Hint: It should be around  $0.18^\circ\text{C}$ .

- **PROBLEM 4:** Suppose you replace the ADC with a 12-bit version operating from 0 to 5V. Re-compute the temperature sensitivity at  $T = 50^\circ\text{C}$ . You can re-use your value of  $dV_{\text{MEAS}}/dT$  from Problem 3. Show all work!
- **PROBLEM 5:** If the self-heating produces a temperature rise less than  $\Delta T_{\text{MIN}}$ , then we can ignore self-heating. Is this the case when using the 8-bit ADC? Assuming a dissipation factor of  $7 \text{ mW}/^\circ\text{C}$  and evaluate the self-heating induced temperature rise at  $T = 30^\circ\text{C}$ . Show all work!

## Another Thermistor Circuit Design

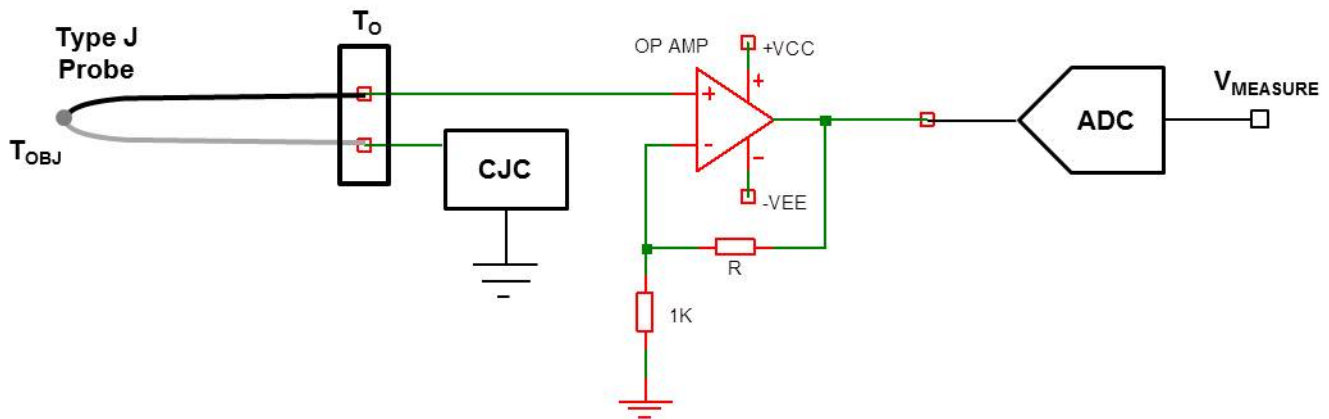
You are asked to design a temperature measurement system that operates from  $0^\circ\text{C}$  to  $+100^\circ\text{C}$ . You decide to use a thermistor  $R_T$  in a quarter bridge powered by  $+5\text{V}$ , as shown in the figure below. The instrumentation amplifier has a differential gain  $A_d = 2$  and is powered by  $+9\text{V}$  and  $\text{GND}$ . The amplifier output is limited to within  $1\text{V}$  of the power supplies (just like in Problem 2). The voltage reference is  $V_{\text{REF}} = +4\text{V}$ . The ADC has 12 bits over a 0 to  $10\text{V}$  range. The system noise voltage is  $10 \text{ mV}_{\text{RMS}}$ . The thermistor properties are the following:

- |                             |                            |   |
|-----------------------------|----------------------------|---|
| • $T = 100^\circ\text{C}$ : | $R_T = 677 \text{ ohm}$    | $\alpha = -2.94 \text{ } \%/^\circ\text{C}$ |
| • $T = 25^\circ\text{C}$ :  | $R_T = 10,000 \text{ ohm}$ | $\alpha = -4.38 \text{ } \%/^\circ\text{C}$ |
| • $T = 0^\circ\text{C}$ :   | $R_T = 32,554 \text{ ohm}$ | $\alpha = -5.09 \text{ } \%/^\circ\text{C}$ |



- **PROBLEM 6:** You have available  $R = 10 \text{ kohm}$  and  $R = 20 \text{ kohm}$ . Do either of these resistors ensure an operating range of  $0$  to  $+100^\circ\text{C}$ ? Show all work!
- **PROBLEM 7:** Compute the temperature sensitivity at  $T = 0^\circ\text{C}$  and  $100^\circ\text{C}$ . Show all work!
- **PROBLEM 8:** Suppose we can ignore self-heating if the temperature rise is less than  $\Delta T_{\text{MIN}}$  at  $T = 0^\circ\text{C}$ . Is this the case? Assume a dissipation factor  $\delta = 5 \text{ mW}/^\circ\text{C}$ . Show all work!

## Thermocouple System



- PROBLEM 9:** Suppose  $T_o = 30^\circ\text{C}$ . What is the appropriate voltage produced by the cold junction compensation? Express your answer in mV. To make things easier, just use the standard Seebeck coefficients from the Lecture 4 notes (see course website). Technically, those values are only for  $0^\circ\text{C}$ , but for this course we'll assume  $\Delta S$  does not change with temperature.
- PROBLEM 10:** What gain  $G$  is necessary to produce a measured voltage  $V_{\text{MEAS}} = (10 \text{ mV}/^\circ\text{C}) \cdot T_{\text{OBJ}}$ ? Hint: See page 4.6 of the lecture notes to guide your thoughts. Hint #2: You should get  $G \approx 196$ .
- PROBLEM 11:** The op amp in the above figure is configured as a non-inverting amplifier (just like Lecture 4). What value of "R" is necessary to achieve a gain  $G$  that is close to your answer in PROBLEM 10? Choose a standard 1% resistor value and compute the actual gain of your amplifier based on this value. For this problem, it does not matter if your actual gain is slightly higher or lower than the ideal value from Problem 10.

NOTE: The pdf on the course website only lists 1% resistor values from 10.0 to 97.6 ohms. Just multiply all values by 10000 if you need resistors between 100 kohm and 976 kohm.

- PROBLEM 12:** Suppose the ADC has 10 bits over a  $\pm 5\text{V}$  range and the noise voltage is  $3 \text{ mV}_{\text{RMS}}$ . Compute the highest temperature  $T_{\text{MAX}}$  that can be measured as well as the temperature sensitivity  $\Delta T_{\text{MIN}}$ . To make things easier, assume the Seebeck coefficient remains constant throughout the temperature range. Also remember to use the actual gain of your amplifier (see Problem 11). Hint:  $T_{\text{MAX}}$  should be near  $500^\circ\text{C}$  and  $\Delta T_{\text{MIN}}$  should be around  $1^\circ\text{C}$ .