

## HW 6: Respiration (10 problems for 100 pts)

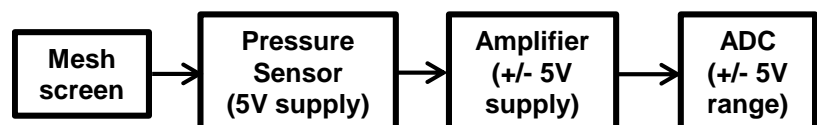
Assume a pneumotachometer has a flow resistance of  $R = 20 \text{ Pa}\cdot\text{s/L}$ , and we want to measure a maximum flow rate of  $16 \text{ L/s}$ . Your instrumentation amplifier is powered by  $+5\text{V}$  and GND with an offset  $V_{\text{ref}} = 1.5\text{V}$ . Assume the amplifier output is limited to  $+4\text{V}$  (max) and  $1\text{V}$  (min). Your ADC operates from  $0$  to  $+5\text{V}$ . Suppose the noise voltage of the measurement system is  $15 \text{ mV}_{\text{RMS}}$ .

- **Problem 1:** Suppose you used a differential pressure sensor with a responsivity  $S = \Delta V / \Delta P = 25 \text{ mV/psi}$ . You must choose either  $A_d = 500, 1000, 1500, 2000$ , or  $2500$ . Which is the best choice?
- **Problem 2:** Compute the number of bits needed to ensure the ADC vertical resolution is smaller than half the noise voltage.
- **Problem 3:** Compute the minimum detectable flow in your system. Express your answer in  $\text{L/s}$ . Hint: You should get  $\Delta F_{\text{MIN}} = 0.1 \text{ L/s}$ .

You are asked to design a Lilly-type spirometer that can measure a maximum flow rate of  $\pm 15 \text{ L/s}$  with a sensitivity of  $\Delta F_{\text{MIN}} = 0.05 \text{ L/s}$ . The mesh screen has a flow resistance  $R = 25 \text{ Pa}\cdot\text{s/L}$ . The instrumentation amplifier has  $V_{\text{ref}} = 0\text{V}$  and is powered with  $\pm 10\text{V}$ , so you can assume the output is limited to  $+9\text{V}$  (max) and  $-9\text{V}$  (min). The ADC operates over a  $\pm 10\text{V}$  span with 12 bits and  $V_{\text{N,RMS}} = 10 \text{ mV}$ .

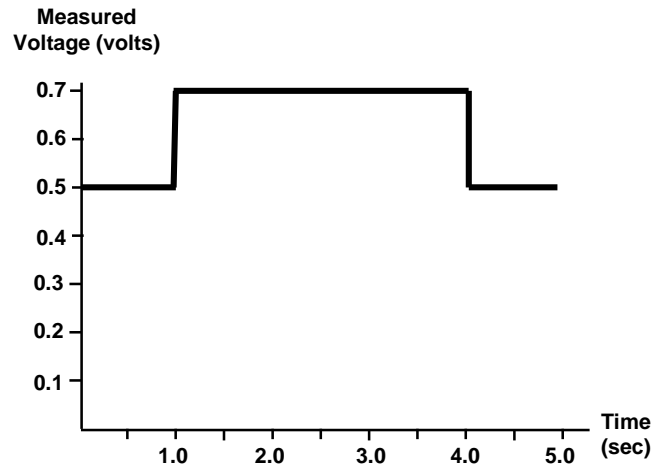
- The two available pressure sensors have a responsivity  $S = \Delta V / \Delta P = 8 \text{ mV/kPa}$  and  $30 \text{ mV/kPa}$ .
- The two available amplifiers have a fixed gain of  $A_d = 1500$  ( $V_{\text{N,RMS}} = 14 \text{ mV}$ ) or  $2500$  ( $V_{\text{N,RMS}} = 20 \text{ mV}$ ).
- You can mix together any components (e.g. Sensor #2, Amplifier #1).
- The total noise from two components (e.g. amplifier + ADC) is computed by:  $V_{\text{N,TOTAL}} = \sqrt{V_{\text{N1}}^2 + V_{\text{N2}}^2}$
- **Problem 4:** What combination of sensor and amplifier is the best choice? Show all work! Hint: You should get Sensor #1 and Amplifier #2.

You are asked to upgrade a flow spirometer system to achieve  $F_{\text{MAX}} = 20 \text{ L/s}$  and  $\Delta F_{\text{MIN}} = 0.05 \text{ L/s}$ .



You know the pressure sensor has  $S = 24 \text{ mV/psi}$  and the instrumentation amplifier has  $A_d = 1500$ . Assume the amplifier output is limited to  $+4\text{V}$  (max) and  $-4\text{V}$  (min).

The current system is calibrated by injecting 3 liters of air into the spirometer over a 3 second interval. The measured voltage  $V_{\text{MEAS}}$  during the calibration is shown to the right.



- Problem 5:** What is the flow resistance  $R$  of the mesh screen? Express your answer in  $\text{Pa}\cdot\text{s/L}$ . Show all work!

Hint #1: First figure out the voltage offset  $V_{\text{REF}}$ .

Hint #2: Remember that  $V_{\text{MEAS}}$  is related to flow, but the syringe injects a known VOLUME.

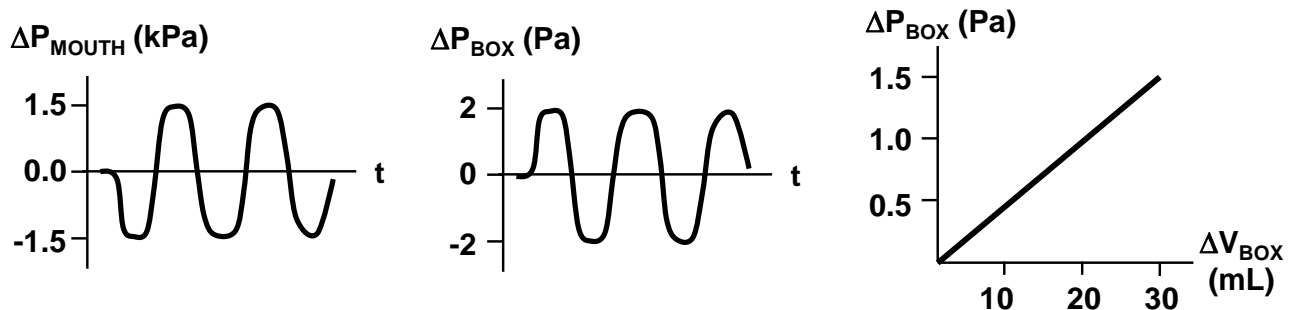
Hint #3: You should get around  $R = 38 \text{ Pa}\cdot\text{s/L}$ .

- Problem 6:** Suppose the amplifier has  $V_{\text{N,RMS}} = 8 \text{ mV}$  and the ADC has 10 bits and  $V_{\text{N,RMS}} = 15 \text{ mV}$ . Does the current system satisfy both design specifications?

The total noise from two components is computed by:  $V_{\text{N,TOTAL}} = \sqrt{V_{\text{N1}}^2 + V_{\text{N2}}^2}$

- Problem 7:** Suppose you also have another amplifier with  $A_d = 1000$  ( $V_{\text{N,RMS}} = 5 \text{ mV}$ ) and the same  $V_{\text{REF}}$ . You also have another ADC with 12 bits and  $V_{\text{N,RMS}} = 4 \text{ mV}$ . Would you replace just the amplifier, just the ADC, or both? Show all work! Hint: You should find that it is necessary to replace both components.

- Problem 8:** Suppose a whole body plethysmography procedure has an initial  $P_{\text{MOUTH}} = 101 \text{ kPa}$ . Plots of  $P_{\text{MOUTH}}$  and  $P_{\text{BOX}}$  during the panting maneuver are shown below. The calibration of  $P_{\text{BOX}}$  is also shown below (right). Compute the FRC. NOTE: Be careful with units (kPa versus Pa)! Hint: Between 2.5 to 3L.



- **Problem 9:** Suppose the helium dilution method is used on a patient. The volume spirometer has a volume of 8L and the initial helium concentration is 7.5%. At the end of the procedure, the final helium concentration is 5.8%. What is the patient's FRC? Hint: Between 2 to 2.5L.
- **Problem 10:** Consider the nitrogen washout technique. The patient's initial N<sub>2</sub> concentration is 9%. The subsequent N<sub>2</sub> measurements are shown below:

	Breath Number											
	1	2	3	4	5	6	7	8	9	10	11	12
Volume	0.40L	0.35L	0.40L	0.40L	0.35L	0.35L	0.45L	0.45L	0.40L	0.35L	0.35L	0.35L
N <sub>2</sub>	8.5%	7.7%	6.9%	6.0%	5.2%	4.4%	3.6%	2.8%	2.0%	1.2%	0.6%	0%

Compute the FRC. Hint: Between 2 to 2.5L.

(End of HW6)