

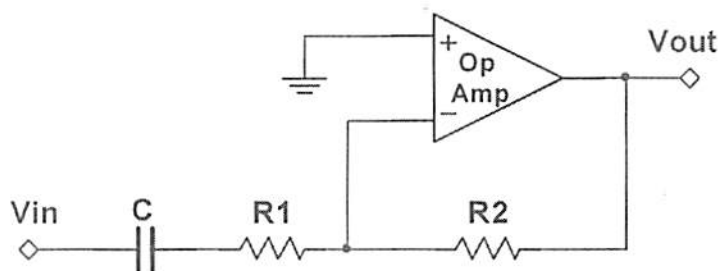
1 problem for 20 pts

ECG Amplifier

You are asked to design an ECG system to monitor a patient in a helicopter (i.e. being flown to a hospital). Suppose the ECG input is a PQRST waveform with a 1 mV amplitude R-wave. The patient's heart rate is 100 beats per minute. This desired signal is superimposed with a constant 25 mV differential offset voltage (e.g. due to skin-electrode impedance mismatch). The helicopter vibration produces a 30 Hz common mode voltage with a peak amplitude of 2.5 V. The instrumentation amplifier has a differential gain $A_d = 30$, CMRR = 75 dB, and $V_{REF} = 0.5V$.

a) Compute and sketch the instrumentation amplifier output over a 3 second interval. Label important features.

b) After the instrumentation amplifier we want a circuit that blocks DC. The op amp circuit shown below combines a high pass filter with an inverting amplifier. Use the Golden Rules to show that:



$$\frac{V_{out}}{V_{in}} = -\frac{R_2}{R_1} \frac{jf/f_c}{1+jf/f_c}$$

NOTE: Make sure to clearly define f_c (i.e. in terms of R_1 , R_2 , and/or C)!

$$CMRR = 20 \log_{10} \left(\frac{A_d}{A_{cm}} \right)$$

(a) $V_{Meas} = V_{Ref} + A_d \Delta V + A_{cm} V_{cm}$

Annotations: $V_{Ref} = 0.5V$, $A_d = 30$, $\Delta V = 25mV + [1mV \text{ PQRST}]$

$$\frac{A_d}{A_{cm}} = 10^{CMRR/20}$$

$$\Rightarrow A_{cm} = \frac{30}{10^{75/20}}$$

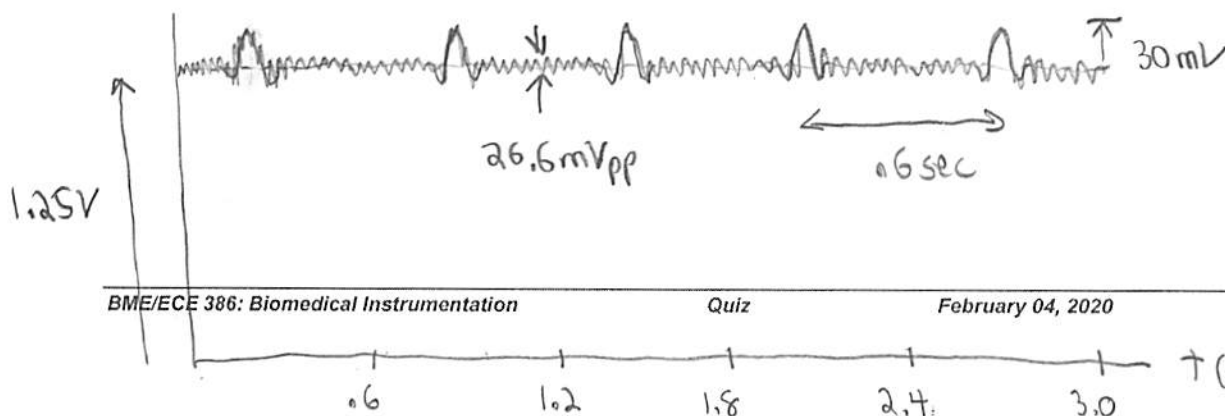
$$2.5 \sin 2\pi f_c t$$

\uparrow 30 Hz

$$= 0.0053$$

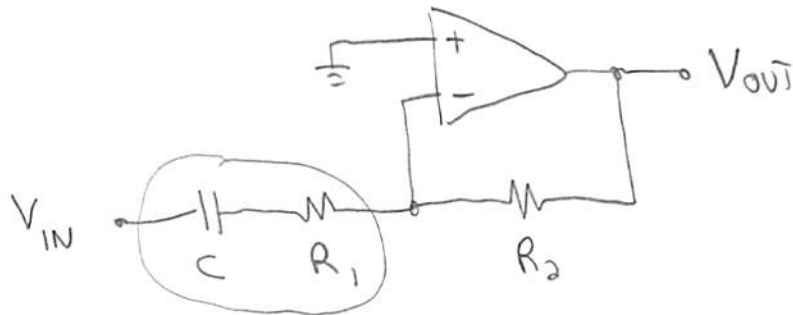
$$\Rightarrow V_{Meas} = .5 + .75 + [30mV \text{ PQRST}] + [13.3mV] \sin 2\pi f_c t$$

$$100 \frac{\text{beats}}{\text{min}} \times \frac{1 \text{ min}}{60 \text{ sec}} \times 3 \text{ sec} = 5 \text{ beats}$$



b)

+10

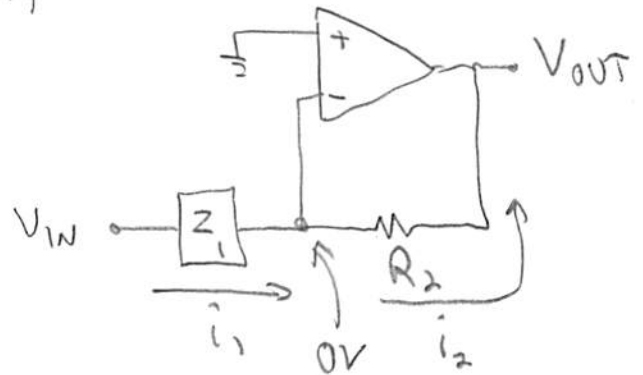


$$Z_1 = \frac{1}{j\omega C} + R_1$$

KCL at node V_- :

$$\hat{i}_1 = \hat{i}_2$$

$$\frac{V_{IN} - 0}{Z_1} = \frac{0 - V_{OUT}}{R_2}$$



$$\frac{V_{OUT}}{V_{IN}} = - \frac{R_2}{Z_1} = - \frac{R_2}{\frac{1}{j\omega C} + R_1} = - \frac{R_2 j\omega C}{1 + j\omega R_1 C} = - \frac{R_2}{R_1} \frac{j\omega R_1 C}{1 + j\omega R_1 C}$$

$$\omega = 2\pi f$$

$$\rightarrow \frac{V_{OUT}}{V_{IN}} = - \frac{R_2}{R_1} \cdot \frac{jf \cdot 2\pi R_1 C}{1 + jf \cdot 2\pi R_1 C}$$

$$\leftarrow \text{Let } \frac{1}{f_c} = 2\pi R_1 C$$

$$f_c = \frac{1}{2\pi R_1 C}$$

$$\boxed{\frac{V_{OUT}}{V_{IN}} = - \frac{R_2}{R_1} \frac{jf/f_c}{1 + jf/f_c}}$$